# Experimental Procedure for Determining the Remanent Magnetic Flux Value Using the Nominal AC Energization

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**Abstract** – The laboratory setup and corresponding experimental procedure for determining the remanent magnetic flux in the magnetic core of a single-phase transformer are presented in this paper. Using the proposed method, the remanent flux can be determined without prior knowledge of any parameter or past states of the transformer which is a significant advantage compared to previously known methods. Furthermore, reliable information about the remanent flux could be obtained using less equipment than other methods. Only electrical measurements are needed, without any physical intervention in the core or some other parts of the transformer. However, the major drawback is that some new unknown value of the remanent flux is set after the measuring procedure. Various initial conditions of the remanent flux and the closing voltage angle are set before each energization of the transformer to prove the validity of the proposed method, which can be used to obtain some characteristics of the remanent flux, such as stability over time or its dependence on some external factors.

Keywords: inductance, magnetic cores, magnetic flux, transformers

### 1. INTRODUCTION

A magnetic core will contain a certain amount of the remanent magnetic flux  $(\Phi_R)$ , also known as residual flux, remanent magnetization or remanence, after the de-energization. An example of a ferromagnetic material's major magnetic hysteresis loop is shown in  $\varphi$ -i characteristics (Fig. 1).



Fig. 1. An example of the magnetic hysteresis loop of a ferromagnetic material

The value of the remanent flux is essential in several areas in practice. One refers to reducing a coil or transformer inrush current by controlled switching [1-4]. Another application area where the remanent flux has an important impact is avoiding current transformer saturation [5-7]. Also, the remanent flux is important as one of the initial conditions in the ferroresonant circuit [8]. In almost all previously mentioned application areas, a magnetic core forms a closed loop, so the remanent flux is closed within the core itself and cannot be measured directly without physical intervention in the core.

However, some methods indirectly determine the remanent flux. The most widely used method is the determination of the remanent flux when de-energizing a coil or transformer by measuring the transformer terminal voltage during the de-energization [8, 9]. The basic idea is to determine the magnetic flux at the instant of de-energization by integrating the port-voltage.

This method is usually used to reduce the inrush current by controlled switching. It is quite simple, but it is unusable if the terminal voltage was not previously measured. Furthermore, the remanent flux can change its value while the coil is not energized if system transients occur [10], or even if there are no external impacts, due to the phenomenon called magnetic viscosity [11]. In that case, the method is unreliable.

Determining the remanent flux can also be done by measuring the leakage flux – the flux near the core is measured and then from the obtained results the remanent flux in the core is estimated [12-14]. Unlike the previous method, all possible changes of the remanent flux after the de-energization are taken into account. Disadvantages are its inaccuracy and high implementation costs – it is challenging to install a magnetic field sensor inside the power transformer tank in an aggressive environment and high temperature. On the other hand, installing the sensor outside the tank will not yield satisfactory results.

The remanent flux can also be determined using the low-voltage DC source for energization [15]. However, an additional DC voltage source is needed to determine the remanent flux utilising this method, while using the proposed method only the nominal voltage source available on-site is required. Furthermore, applying this method, the major hysteresis loop of the observed transformer needs to be obtained before determining the remanent flux, which is not the case in the proposed method. This method can be used in the same application areas as the proposed method.

The remanent flux could also be determined using the inductance value of the winding of a transformer [16]. As in [15], the transformer should be tested before using this method, and the correlation between the remanent flux and the inductance must be established. The conclusion is that the inductance will decrease if the remanent flux is high. However, this method is quite inaccurate – if the remanent flux value changes from zero to the maximum value, the inductance will change only 5% of its value.

Furthermore, the remanent flux could be determined using a minor hysteresis loop without any data regarding the last de-energization [17]. However, the transformer should be tested before using this method, and the relation between the remanent flux and the parameter WQ has to be established. But, it could be used for reducing the inrush current by controlled switching because the determined remanent flux will be preserved after the measurement process.

Finally, there is the method for determining the remanent flux which uses the nonlinear magnetizing characteristics of the core [18]. The basic idea is to energize a coil or transformer with the low voltage DC source and analyze the transient current. Prior to application of the method, the observed transformer should be tested and transient currents should be obtained for all possible remanent flux values. However, after applying this method, some unknown value of the remanent flux after the determination will be established.

There are also demagnetization and prefluxing techniques which actually do not determine the remanent flux, but set it to zero and the maximum value, respectively [19-21]. The basic idea of prefluxing is to set the remanent flux to the maximum positive or negative value prior to operation [22-25]. After demagnetization or prefluxing, the optimal switching angle for reducing the inrush current can easily be calculated. The devices used for demagnetization and prefluxing are simple in construction and operate using low DC voltage.

There is no adequate method for determining the remanent flux which can obtain some features, such as stability over time or how it is influenced by some external factors, except the method shown in [15]. Most of the previously mentioned methods cannot give satisfactory results regarding the precise and reliable value of the remanent flux in a closed magnetic core.

The laboratory setup and corresponding method for determining the remanent flux value will be presented in this paper. Although this paper will discuss only the remanent flux in the transformer core, the proposed method could also be appropriately applied to the iron core coil.

In most cases in practice, the possibility of setting the remanent flux to any value is not used for mitigating inrush current, due to the fact that setting magnetic flux value requests additional devices [20-24]. Thus, the methods most often used rely on integrating the measured port-voltage during the de-energization and assuming that the determined remanent flux will not change until the subsequent energization [2, 3, 9, 26]. The proposed method could be used to check this assumption, where one could consider the timedependence of the remanent flux. In some cases, the time interval between de-energization and the next energization of the power transformer or coil (e.g. used for compensation of reactive power) could be a couple of months. Furthermore, it is proven that the remanent flux in the core can be changed even if the transformer is not energized [10]. Thus, using the proposed method, it can be investigated how system transients and external magnetic fields affect the remanent flux.

Finally, the remanent flux can be determined without any data about the past states. Furthermore, the parameters of the transformer, except the nominal voltage, should not be known. Only the voltage and current measurements should be conducted, meaning less equipment is required than in the other methods.

#### 2. PROPOSED METHOD

The simple model of the winding of an unloaded transformer can be used as shown in Fig. 2 inside the dashed rectangle.



Fig. 2. The model of the winding of an unloaded transformer

The model consists of a linear resistance R in a series with a nonlinear inductance L with  $\varphi$ -i characteristics (Fig. 1) experimentally obtained. The resistance R represents the winding resistance. The model shown in Fig. 2 uses the  $\varphi$ -*i* characteristics of an unloaded transformer which including nonlinear characteristics with hysteresis. However, only the major magnetic hysteresis loop which is obtained for particular excitation (AC voltage, RMS 39 V, 50 Hz) is defined. The operating point or trajectory could be anywhere inside the loop for some arbitrary excitation. This makes the simulation model appropriate only for the steady state established for the previously mentioned excitation. However, there are some other models more appropriate for simulation, such as the lumped-circuit model by Chua and Stromsmoe [27], the Preisach model [28] and the Jiles-Atherton model [29]. The Chua mathematical model could not be used for the remanent flux simulation, because its nonlinear characteristics of the inductance and resistance are anhysteretic. On the other side, the Preisach and Jiles-Atherton models can be used to explain the remanent flux phenomenon as shown in [30] for the Preisach model. However, even if it is inappropriate for simulation in general, the role of model (Fig. 2) in this paper is to clarify the rationale behind our experimental procedure. Thereby, due to the straightforward physical explainability of the model, it was not necessary, given the focus of this paper, to use simulation as additional validation of the experiment. Our future research will address various already mentioned modeling and simulation methods, but also FEM and BEM modelling [31].

Assume that the AC source voltage is

$$u = U \sin \omega t. \tag{1}$$

Kirchhoff's voltage law for the model shown in Fig. 2 equals

$$iR + N \frac{d\varphi}{dt} = \hat{U} \sin \omega t.$$
 (2)

In the steady state, (2) for the DC components can be expressed as

$$I(0)R + N\frac{d\Phi(0)}{dt} = U(0), \qquad (3)$$

where I(0),  $\Phi(0)$  and U(0) are the DC components of the magnetizing current (*i*), the magnetic flux ( $\varphi$ ) and the AC source voltage (u), respectively. Considering that the DC component of the AC source voltage, U(0), is zero and concerning (3), the DC component of the magnetizing current, I(0), must also be zero because  $\Phi(0)$  has a constant value per definition and, thus, its derivative equals to zero.

Furthermore, considering that the magnetic flux  $(\varphi)$  is an odd function of the magnetizing current (i), as shown in Fig. 1, the DC component of the magnetic flux,  $\Phi(0)$ , in the steady state must also be zero.

The basic idea is to energize the unloaded transformer at the nominal AC voltage and measure the magnetizing current (*i*) and inductance voltage ( $u_{i}$ ). The inductance voltage can be obtained as the difference between the measured transformer terminal voltage (u) and the product of the current (*i*) and the resistance (R):

$$u_L = u - iR. \tag{4}$$

Furthermore, the inductance voltage (uL) can also be obtained by measuring the voltage on the secondary unloaded winding and converting it to the primary side using the turns ratio. The magnetic flux ( $\phi$ ) in the core equals

$$\varphi(t) = \frac{1}{N} \int_{0}^{t} u_{L}(\tau) d\tau + \Phi_{R}, \qquad (5)$$

where *N* is the number of the corresponding transformer winding turns, *t* and  $\tau$  are the time variables, and  $\Phi_R$  is the remanent flux value, that is, the magnetic flux at instant *t* = 0. Considering (5), the DC component of the magnetic flux ( $\varphi$ ) in the steady state can be expressed as

$$\Phi(0) = \frac{1}{T} \int_{t_{ss}}^{t_{ss}+T} \left[ \frac{1}{N} \int_{0}^{t} u_{L}(\tau) d\tau + \Phi_{R} \right] dt,$$
(6)

where *T* is the period of the AC source voltage. Considering that the DC component of the magnetic flux,  $\Phi(0)$ , in the steady state must be zero and concerning (6), the remanent flux ( $\Phi_p$ ) equals

$$\Phi_{R} = -\frac{1}{T} \int_{t_{ss}}^{t_{ss}+T} \left[ \frac{1}{N} \int_{0}^{t} u_{L}(\tau) d\tau \right] dt,$$
(7)

Whereby it is crucial to choose the period for calculating the DC component in the steady state, not during the transient state. In other words, the instant  $t_{ss}$  must be in a steady state. Consequently, the remanent flux  $(\Phi_R)$  can be obtained using the measured inductance voltage  $(u_I)$ , that is, the calculated magnetic flux  $(\varphi_C)$ :

$$\Phi_{R} = -\frac{1}{T} \int_{t_{ss}}^{t_{ss}+T} \varphi_{C}(t) dt, \qquad (8)$$

$$\varphi_{C}(t) = \frac{1}{N} \int_{0}^{t} u_{L}(\tau) d\tau.$$
(9)

#### 3. LABORATORY SETUP

The measurement circuit with the model shown in Fig. 3 is built to determine the remanent flux  $(\Phi_{R})$  by analyzing the unloaded transformer's inductance voltage  $(u_{L})$  waveform. Various initial conditions of magnetic flux at the moment of de-energization (de-energization)

gization flux,  $\Phi_{D}$  and the closing voltage angle ( $\alpha$ ) will be set to prove the validity of the proposed method independently of the initial conditions.



Fig. 3. The measurement circuit model

The measurement circuit model consists of the two winding transformer (inside the dashed rectangle), the resistance  $R_{R'}$  three variable AC voltage sources,  $u_1$ ,  $u_2$  and  $u_3$ , two electronically controlled switches  $S_1$  and  $S_2$ , and the ordinary mechanical switch  $S_3$ . The transformer is modeled with the resistance  $R_T$  and the perfect transformer (ideal transformer with magnetizing inductance L included) connected in a series (Fig. 3). The magnetic characteristics of the nonlinear inductance L are shown in Fig. 1. Physical realization of the measurement circuit is shown in Fig. 4.



Fig. 4. Realization of the measurement circuit

The measurement circuit consists of: 1 – transformer under test, 2 – resistor  $R_{R'}$  3 – electronic switching device, 4 – PC with installed data acquisition software, 5 – data acquisition card, 6 and 7 – active differential probes, 8 – passive voltage probe, 9 – oscilloscope, 10 – current probe, 11 – digital multimeters, 12 – variable AC voltage source  $u_1$  used for the energization of the transformer, 13 – variable AC voltage source  $u_2$  used for the setting of the de-energization flux, 14 – variable AC voltage source  $u_3$  used for demagnetization.

The single-phase transformer (1, Fig. 4) is made of a toroidal core with two windings – 47 and 7 turns, both wired with triple wire (each has a round cross-section of 1.3 mm<sup>2</sup>). The magnetic core (the cross-sectional area is 20 cm<sup>2</sup>) consists of oriented transformer sheets (M5-type). The nominal power is 200 VA, nominal voltages are 30 V and 4.5 V, and nominal currents are 6.5 A and 44.5 A. The resistor  $R_{\tau}$  equals 0.19  $\Omega$  and inductance *L* equals 0.59 H in linear (non-saturated) area (Fig. 3). The purpose of the resistor  $R_{\mu}$  which equals 1.22  $\Omega$  (2, Fig. 4, also shown in

Fig. 3) is to limit the inrush current. If not used, it could reach up to 120 A, devastating for the equipment used. The secondary winding terminals are used only for obtaining the voltage  $(u_{c})$ . The electronic switching device (3, Fig. 4) sets the initial remanent flux. All the measured values (magnetizing current, primary and secondary voltage) are obtained using the data acquisition (DAQ) card National Instruments NI-USB 6212 (5, Fig. 4) and the PC (4, Fig. 4). The waveform of the magnetizing current (i) is obtained indirectly by measuring the voltage on the additional resistor  $(R_p)$  using active differential probe GW Instek GDP-025 (6, Fig. 4). Furthermore, the primary voltage  $(u_p)$  is also obtained using active differential probe (7, Fig. 4) and the secondary voltage  $(u_s)$  using passive differential probe (8, Fig. 4). The sampling frequency was set to 50 kHz. The frequency of all the AC sources is 50 Hz. Furthermore, oscilloscope (9, Fig. 4) and digital multimeters (11, Fig. 4) were used only for monitoring the situation. All the measuring data used in this research is collected using the DAQ card and PC.

## 4. EXPERIMENTAL PROCEDURE

Every single measurement is carried out in three steps, but only to test the proposed method's validity. In possible application, only the third step of the experimental procedure should be carried out. The first step is AC demagnetization, carried out by slowly decreasing the voltage of the variable AC source  $u_3$  from the RMS value of 36 V to zero in approximately 10 s, as shown in [32]. During the core demagnetization, the switches  $S_1$  and  $S_2$  are open. The demagnetization is important for setting the de-energization flux ( $\Phi_p$ ) value in the second step.

The second step follows up approximately 5 s after the first step, and it is done using the AC source  $u_2$  and the switch  $S_2$ , while the switches  $S_1$  and  $S_3$  are open. The second step is described in detail in [15]. The value of the de-energization flux ( $\Phi_D$ ) is set by changing the RMS voltage of the variable AC source  $u_2$  ( $U_2$ ) and the instant of opening the switch  $S_2$  (when the current is crossing zero value). In total, 25 different de-energization flux values are obtained in this experiment which corresponds to 13 different RMS voltages of the variable AC source  $u_2$ ( $U_2$ ), including zero value, and two different zero crossings of the magnetizing current in the  $\varphi$ -*i* characteristics. De-energization flux ( $\Phi_D$ ) values and corresponding RMS voltages  $U_2$  are shown in Table 1. (only positive values due to the symmetry of the  $\varphi$ -*i* characteristics).

**Table 1.** Corresponding de-energization flux values and RMS voltages of the variable AC source  $u_2$ .

U <sub>2</sub> (V)	${oldsymbol{\Phi}}_{_{D}}$ (mVs)	$U_{_2}(\mathbf{V})$	$\Phi_{_D}$ (mVs)
36	2.997	18	1.152
33	2.752	15	0.901
30	2.364	12	0.650
27	2.040	9	0.433
24	1.728	б	0.140
21	1.441	3	0.061

The third step follows up in less than 1 s after the second step. Thus, the value of the set de-energization flux  $(\Phi_{\rm p})$  will be considered as the value of the remanent flux  $(\Phi_{\nu})$  in the core in the moment of energization of the transformer in the third step. This is the usual procedure when determining the remanent flux during the de-energization of the transformer by measuring the port-voltage [33, 34]. The third step of the experimental procedure is the only step which will be carried out in the possible application of the proposed method, and it is energizing the transformer using the AC source  $u_1$  and the electronically controlled switch  $S_1$ , while the switches  $S_2$  and  $S_3$  are open. The RMS voltage of the AC source  $u_1$  is set to 36 V which is 20% higher than the nominal voltage of the primary winding. It is done to obtain the steady state faster. Namely, the time constant that affects the length of the transient state is L/(RT+RR) whereby the inductance L is not a constant value, but equals

$$L = \frac{d\varphi}{di}.$$
 (10)

Thus, when the core reaches saturation, the inductance L is significantly lower than in the non-saturated region. Finally, the lower inductance L, the lower time constant means faster entry in the steady state. This is important because the remanent flux  $(\Phi_p)$  value is obtained as the negative value of the DC component of the calculated magnetic flux ( $\varphi_{c}$ ) in the steady state. The closing voltage angle ( $\alpha$ ), is set by the PC over the electronically controlled switch  $S_1$ . To prove that the different initial conditions of the de-energization flux ( $\Phi_{p}$ ) and closing voltage angle ( $\alpha$ ) do not affect the validity and accuracy of the proposed method, the measurements were carried out by varying the following parameters:

•  $U_2 = 36 \text{ V} (-), 33 \text{ V} (-), ..., 0 \text{ V}, ..., 33 \text{ V} (+), 36 \text{ V} (+);$ •  $\alpha = 0^\circ, 30^\circ, 60^\circ, 90^\circ, 120^\circ, 150^\circ, 180^\circ;$ 

which in total gives 175 measurements. At the end, the obtained values of the remanent flux using the proposed method will be compared to the set values of the de-energization flux.

#### 5. EXPERIMENTAL RESULTS

The obtained results for each measurement include the magnetizing current (i), the primary winding voltage  $(u_p)$ , the secondary winding voltage  $(u_c)$ , and the calculated magnetic flux ( $\varphi_c$ ). Examples of the obtained waveforms are shown in Figs. 5, 6, 7, and 8, respectively.



**Fig. 5.** Magnetizing current (*i*) for  $U_2 = 18 V (+)$ and  $\alpha = 90^{\circ}$ 



**Fig. 6.** Primary winding voltage  $(u_p)$  for  $U_2 = 18 V (+)$ and  $\alpha = 90^{\circ}$ 



**Fig. 7.** Secondary winding voltage  $(u_s)$  for  $U_2 = 18$  V (+) and  $\alpha = 90^{\circ}$ 



**Fig. 8.** Calculated magnetic flux ( $\varphi_c$ ) for  $U_2 = 18$  V (+) and  $\alpha = 90^{\circ}$ 

For each measurement, the remanent flux  $(\Phi_p)$  value is obtained as the negative value of the DC component of the calculated magnetic flux ( $\varphi_c$ ) in the steady state. The obtained remanent flux  $(\Phi_{R})$  values are shown in Table 2, where parameter  $U_2$  is marked with its value and sign (+) or (-) attached, depending on the sign of the set de-energization flux  $(\Phi_p)$ .

Table 2. Obtained remanent flux values

RMS	Closing voltage angle, $\alpha$						
voltage, U <sub>2</sub> (V)	<b>0</b> °	<b>30</b> °	<b>60</b> °	<b>90</b> °	120°	150°	1 <b>80</b> °
36 (+)	3.082	3.083	3.085	3.080	3.078	3.079	3.077
33 (+)	2.752	2.788	2.757	2.747	2.748	2.751	2.766
30 (+)	2.123	2.179	2.164	2.369	2.330	2.178	2.337
27 (+)	1.805	1.881	2.104	2.078	1.872	1.864	2.055
24 (+)	1.605	1.721	1.557	1.705	1.664	1.750	1.609
21 (+)	1.323	1.455	1.378	1.344	1.536	1.309	1.242
18 (+)	1.160	1.326	1.041	1.018	1.252	1.189	1.280
15 (+)	1.004	1.072	0.868	1.026	0.913	0.864	0.892
12 (+)	0.584	0.508	0.606	0.687	0.544	0.645	0.650
9 (+)	0.377	0.378	0.445	0.370	0.454	0.353	0.429
6 (+)	0.273	0.331	0.339	0.310	0.340	0.312	0.267
3 (+)	0.167	0.163	0.186	0.151	0.181	0.143	0.148
0	-0.049	0.002	0.002	0.013	0.051	-0.037	-0.023

RMS			Closing	voltage	angle, $\alpha$		
voltage, U <sub>2</sub> (V)	<b>0</b> °	<b>30</b> °	<b>60</b> °	<b>90</b> °	120°	150°	180°
3 (–)	-0.155	-0.128	-0.130	-0.139	-0.140	-0.156	-0.151
6 (–)	-0.308	-0.263	-0.278	-0.270	-0.307	-0.342	-0.335
9 (–)	-0.443	-0.386	-0.339	-0.457	-0.381	-0.438	-0.430
12 (–)	-0.714	-0.738	-0.713	-0.692	-0.644	-0.801	-0.614
15 (–)	-0.992	-0.756	-0.802	-0.974	-0.879	-0.887	-0.988
18 (–)	-1.065	-1.126	-1.087	-0.917	-1.006	-1.099	-1.239
21 (–)	-1.458	-1.261	-1.195	-1.447	-1.361	-1.360	-1.208
24 (–)	-1.543	-1.660	-1.771	-1.731	-1.502	-1.591	-1.847
27 (–)	-1.848	-1.825	-1.837	-2.067	-1.850	-2.054	-1.916
30 (–)	-2.159	-2.243	-2.295	-2.180	-2.238	-2.115	-2.291
33 (–)	-2.725	-2.735	-2.727	-2.702	-2.690	-2.749	-2.731
36 (–)	-3.051	-3.049	-3.028	-3.043	-3.048	-3.055	-3.057

For each parameter of  $U_2$ , the obtained remanent flux  $(\Phi_R)$  value should be the same, regardless of the initial condition of the closing voltage angle ( $\alpha$ ). To evaluate this, for each parameter of RMS voltage  $U_2$ , the average remanent flux value ( $\Phi_{R,average}$ ) is calculated as

$$\Phi_{R_average} = \frac{\sum_{i=1}^{n} \Phi_{Ri}}{7}.$$
(11)

Also, the standard deviation ( $\sigma$ ) of the obtained remanent flux ( $\Phi_R$ ) values for each parameter of RMS voltage  $U_2$  is calculated as

$$\sigma = \sqrt{\frac{\sum_{i=1}^{7} \left(\Phi_{R_i} - \Phi_{R_average}\right)^2}{6}}.$$
 (12)

Furthermore, the relative standard deviation ( $\sigma_{_{\%}}$ ) is calculated for each parameter of  $U_{_{2}}$  as

$$\sigma_{\%} = \frac{\sqrt{\frac{\sum_{i=1}^{7} \left(\Phi_{Ri} - \Phi_{R_{average}}\right)^{2}}{6}}}{\Phi_{R_{average}}} \cdot 100 \%.$$
(13)

**Table 3.** Standard deviation and relative standard deviation of the obtained remanent flux values

RMS voltage U <sub>2</sub> (V)	Average remanent flux value, Ø <sub>R</sub> _average (mVs)	Standard deviation, σ (mVs)	Relative standard deviation, $\sigma_{_{\%}}$
36 (+)	3.080	0.003	0.09%
33 (+)	2.759	0.014	0.49%
30 (+)	2.240	0.093	4.17%
27 (+)	1.951	0.114	5.82%
24 (+)	1.659	0.066	3.95%
21 (+)	1.370	0.091	6.63%
18 (+)	1.181	0.109	9.19%
15 (+)	0.949	0.078	8.21%
12 (+)	0.603	0.058	9.69%
9 (+)	0.401	0.037	9.35%
6 (+)	0.310	0.028	9.01%
3 (+)	0.163	0.015	9.42%

0	-0.006	0.031	535.62%
3 (–)	-0.143	0.011	7.43%
6 (–)	-0.300	0.029	9.63%
9 (–)	-0.410	0.039	9.60%
12 (–)	-0.702	0.057	8.06%
15 (–)	-0.897	0.087	9.69%
18 (–)	-1.077	0.092	8.59%
21 (–)	-1.327	0.100	7.51%
24 (–)	-1.664	0.117	7.03%
27 (–)	-1.914	0.097	5.06%
30 (–)	-2.217	0.063	2.84%
33 (–)	-2.723	0.019	0.69%
36 (–)	-3.047	0.009	0.30%

The measurement results show that the relative standard deviation ( $\sigma_{\rm sc}$ ) does not exceed 10% in any case, except for  $U_2 = 0$  V. That exception is because the denominator value (average remanent flux) is near zero when calculating the relative standard deviation ( $\sigma_{\omega}$ ). Also, the relative standard deviation ( $\sigma_{\omega}$ ) lowers when the RMS voltage  $U_2$  rises. The reason for these deviations could be in the second step of the experimental procedure when magnetizing the transformer, that is, setting the de-energization flux  $(\Phi_p)$ . In the first step of the experimental procedure, the transformer is demagnetized and this is done accurately. But the second step is critical in terms of accuracy, especially at lower magnetizing voltage values. At higher magnetizing voltage values, the relative standard deviation ( $\sigma_{\alpha}$ ) is less than 1%. In these cases, the transformer goes into saturation even at the steady state, while at lower magnetizing voltage values it does not go into saturation at all. So, at lower magnetizing voltage values, the transformer will slowly enter a steady state because of the higher time constant in these cases. As a result, the magnetizing process in the second step does not always set the aimed de-energization flux ( $\Phi_p$ ) value accurately.

Finally, the obtained average remanent flux values for each parameter  $U_2$  are compared to the corresponding de-energization flux ( $\Phi_p$ ) values shown in Table 1. The results are shown in Fig. 9.



Fig. 9. Obtained average remanent flux values and corresponding de-energization flux values for each parameter of RMS voltage  $U_2$ 

The obtained average remanent flux value is almost the same as the corresponding de-energization flux value for each parameter  $U_2$ , as shown in Fig. 9. Also, symmetry of the results can be seen in Fig. 9, which is the expected result because of symmetrical  $\varphi$ -*i* characteristics. The ratios of the obtained average values of remanent flux ( $\Phi_R$ ) and corresponding values of de-energization flux ( $\Phi_n$ ) are shown in Table 4 for each parameter  $U_2$ .

# **Table 4.** Ratios of the obtained average values ofremanent flux and corresponding valuesof de-energization flux

<i>U</i> <sub>2</sub> ( <b>V</b> )	Remanent flux / De-energization flux	<i>U</i> <sub>2</sub> ( <b>V</b> )	Remanent flux / De-energization flux
36 (+)	102.79%	36 (–)	101.69%
33 (+)	100.23%	33 (–)	98.93%
30 (+)	94.74%	30 (–)	93.78%
27 (+)	95.65%	27 (–)	93.80%
24 (+)	95.97%	24 (–)	96.25%
21 (+)	95.01%	21 (–)	92.07%
18 (+)	102.47%	18 (–)	93.46%
15 (+)	105.28%	15 (–)	99.55%
12 (+)	92.88%	12 (–)	108.08%
9 (+)	92.56%	9 (–)	94.81%
6 (+)	222.05%	6 (–)	214.98%
3 (+)	266.70%	3 (–)	233.93%

The results in Table 4 show that the average remanent flux values are between 93% and 108% of the corresponding values of de-energization flux in most cases. The exceptions appear only for parameters with RMS voltage  $U_2 = 3 V(+)$ ,  $U_2 = 3 V(-)$ ,  $U_2 = 6 V(+)$ , and  $U_2 = 6 V(-)$ . The reason for these exceptions could be the relatively small absolute values of the obtained remanent flux and corresponding de-energization flux which can cause higher measurement uncertainty. Another reason could be the imprecise setting of the de-energization flux in the second step of the experimental procedure.

#### 6. CONCLUSION

The remanent flux can be determined using the presented experimental procedure without any data about parameters or past states of a transformer, using only electrical measurements. Some of the previously mentioned methods determine the remanent flux during the de-energization, which is very useful for reducing the inrush current by controlled switching. However, most of these methods cannot be used for investigating stability over time and the impact of the external excitations (system transients and magnetic fields) on the remanent flux in the core because they determine it in the moment of de-energization. Namely, those external excitations could change the remanent flux value while the transformer is not even connected to the grid. This means that the remanent flux can have a different value at the end of such an idle state, compared to the deenergization instant. On the other hand, the proposed method determines the remanent flux in the moment of energization of the transformer, that is, after an idle state. This means that the proposed method is unusable for reducing the inrush current by controlled switching because some new value of the remanent flux is established in the core after conducting the experimental procedure. It also means that the determined value will depend on the moment of the previous de-energization. Still, every change of the remanent flux between the previous de-energization and new energization will be taken into account, contrary to the other methods of determination during the de-energization. Thus, some new value of the remanent flux is established in the core after conducting the proposed method, but in investigating the stability over time and impacts of external excitations on the remanent flux, this drawback is not crucial because the goal is to determine how remanent flux was changed during the idle state, that is, its new value established at the end of the experimental procedure is not significant. Although there is a method similar to the proposed one which uses the low voltage DC source to determine the remanent flux, the proposed method could be more applicable because it uses the nominal voltage for energization, which could be easier to obtain on-site. Furthermore, the proposed method does not demand any data about the observed transformer, except the nominal voltage, which is not the case when using the method with the DC energization.

Finally, the other methods which determine the remanent flux during de-energization and the proposed method go along in investigating the stability over time and impacts of external excitations on the remanent flux. Namely, using the previously known methods, the remanent flux will be determined in the moment of deenergization and using the proposed method, the remanent flux will be determined in the moment of new energization, enabling comparison of these two values, that is, detecting the remanent flux changes due to the impact of external excitations.

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