# Multilevel Thresholding of Brain Tumor MRI Images: Patch-Levy Bees Algorithm versus Harmony Search Algorithm

Preliminary Communication

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**Abstract** – Image segmentation of brain magnetic resonance imaging (MRI) plays a crucial role among radiologists in terms of diagnosing brain disease. Parts of the brain such as white matter, gray matter and cerebrospinal fluids (CFS), have to be clearly determined by the radiologist during the process of brain abnormalities detection. Manual segmentation is grueling and may be prone to error, which can in turn affect the result of the diagnosis. Nature inspired metaheuristic algorithms such as Harmony Search (HS), which was successfully applied in multilevel thresholding for brain tumor segmentation instead of the Patch-Levy Bees algorithm (PLBA). Even though the PLBA is one powerful multilevel thresholding, it has not been applied to brain tumor segmentation. This paper focuses on a comparative study of the PLBA and HS for brain tumor segmentation. The test dataset consisting of nine images was collected from the Tuanku Muhriz UKM Hospital (HCTM). As for the result, it shows that the PLBA has significantly outperformed HS. The performance of both algorithms is evaluated in terms of solution quality and stability.

Keywords – Brain MRI, HS, multilevel thresholding, Otsu, PLBA, segmentation.

# 1. INTRODUCTION

Cancer is the second mortality causing factor in the world with 8.8 million cases reported as of 2015 [1]. In Malaysia, cancer is the third highest contributor to mortality [2]. Categorically speaking, Malays have the highest survival rate among those affected by brain and nervous system cancers, which amounts to 43%, as reported by the Malaysian Study on Cancer Survival (MySCan), 2018. This has become the second highest rate in terms of survivors, with ovarian cancer (54.8%) and stomach cancer (27.6%) being is the first and the third, respectively [1]. Indians and Chinese have the highest survival percentage in other types of cancer [1]. It can be concluded that Malays have a higher risk of developing brain cancer in Malaysia.

Brain tumor or brain cancer is a cluster of abnormal cells in the human brain [3]. There are two types of tumors, namely malignant (cancerous) and benign (non-cancerous) [3]. Medical imaging is an important medium for radiologists to accurately diagnose brain disease such as cancer. High resolution MRI of the brain is needed for better brain tumor detection.

The advantage of MRI is that it is the least risky method for constructing data with spatial resolution in high scale and non-invasive modality compared to other techniques of diagnostic imaging [4]. There are several methods that have been applied successfully in MR image segmentation.

Manual segmentation of MRI images is arduous, expensive and time consuming. Any mistake is susceptible due to blurriness on tissues boundaries, low tissue contrast and poor hand-eye coordination. Consequently, discrepancies are common among radiologists determining a variety of structures. Therefore, a plethora research studies were introduced to increase the accuracy of brain tissues segmentation upon brain disease diagnosis.

Effective brain MRI segmentation can improve a classification of brain diseases with better precision. Joliot et al. [5] proposed a technique of three-dimensional automatic segmentation that separates gray level thresholding of gray matter and white matter. In fact, brain MRI images occasionally have some noise component as a result of patient movement during brain scanning. Raquel et al. [6] introduced a hybrid model for multispectral brain MRI segmentation based on a radial basic network. This method falls short of solving the brain MRI images with noise. To overcome this problem, a clustering method is put forth.

In a number of pixel-based approaches, the clustering method has the most prominent application in terms of image segmentation [7]. In the last decade, clustering-based approaches garnered significant interest in the domain of medical imaging. The fuzzy cmeans (FCM) clustering algorithm was introduced by Bezdek [8] to minimize an objective function which is known as fuzzy membership and a set of cluster centroids. However, FCM still blunders in separating the pixel since it contains noisy pixels.

Histogram-based thresholding is a very popular tool in image segmentation. Bi-level thresholding is also known as the simplest problem compared to multi-level thresholding. Bi-level thresholding segments the image into two groups. If the image consisting of a gray-pixel level is higher than the threshold, it is defined as one group. Otherwise, it is included as another group. In the case of multilevel thresholding, it is more challenging to define a group of pixels when more details of segmentation are produced. Determining distinct valleys in a multilevel histogram is no easy task. Hence, the problem of multilevel thresholding has become the point of interest among researchers.

Otsu's method [9], which is also known as a nonparametric approach, selects optimal thresholds by maximizing the between-class variance of gray levels. Gray levels of the image are normally distributed [10]. This method is easy and powerful in bi-level thresholding [10]. Otsu's method can possibly be applied in multilevel thresholding. However, it is significantly formidable to determine optimal thresholds due to exponential growth in computation time. Owing to that, numerous methods for solving the multilevel thresholding problem have been proposed [11].

Multilevel thresholding-based metaheuristics is proposed by the researchers to increase search speed as it has been attested to yield the best result in (optimal) thresholds. Brain MRI segmentation focuses on the normal brain by using bacterial foraging optimization (BFO) [12], a genetic algorithm (GA) [13], and adaptive bacterial foraging optimization (ABF) [14], which have been successfully implemented.

Brain tumor MRI images encompass various artifacts such as cyst, solid and edema. Multilevel thresholding of brain tumor MRI images segmentation is also successfully applied based on metaheuristic methods such as harmony search (HS) [15]. The advantage of the Patch-Levy Bees Algorithm (PLBA) is that it is more realistic and it is attained by speeding up the search process to find an optimal threshold based on multilevel thresholding for image segmentation [16]. The PLBA has never been applied in brain MRI segmentation. Owing to that, compared to HS, the PLBA is deemed interesting for the application in brain tumor MRI images, by using the recent methods to provide better brain tumor image segmentation.

# 2. IMAGE THRESHOLDING

Image thresholding is one of the types of image segmentation techniques. It segments an image into different intensity levels of color or gray images. Image segmentation through image thresholding is the most convenient and effortless method effortless. Threshold values are the intensity values selected from the color or gray intensities of the image. Based on selection of these threshold values, an image is segmented into different regions.

# 2.1. GLOBAL THRESHOLDING

Global thresholding has one threshold to segment into two partitions [17]. It operates in such a way that if any gray value of images is higher than the threshold value, it will join into one group; otherwise, it will join into the other group. Even though global thresholding is so easy to implement, it only considers segmentation of the image into two partitions. It may suffer from the loss of sharp pixels to classify in the image whose color intensities are more similar to other uniquely classified pixels. The global thresholding method is also known as a bi-level thresholding method.

## 2.2. MULTILEVEL THRESHOLDING

Multilevel thresholding considers segmentation of more than one threshold value into several groups [17]. The number of segmented images is one more than the number of threshold values chosen. It can be concluded that if three threshold values are selected, it will produce four groups of regions for the segmented image. Generally, some of the sharp pixels that went through global thresholding may be lost or missing after performing segmentation separately. For the purpose of solving the shortcomings of global thresholding, multilevel thresholds are selected.

Gray images have L levels of gray in the range (0, 1, 2, ..., L-1 1). Let h(1), h(2),..., h(L-1), be the observed graylevel frequency. The probability of occurrence of the gray level i can be defined as in (1):

$$P_{i} = \frac{h(i)}{N} for \ (0 \le i \le L - 1), \tag{1}$$

where h(i) is the number of pixels corresponding to the gray level *i* and N is the total number of pixel in the image, which is equal to  $\sum_{i=0}^{L-1} h(i)$ 

# 3. BRIEF DESCRIPTION OF THE COMPARED ALGORITHMS

## 3.1. HARMONY SEARCH

Harmony search (HS) was introduced by Geem in 2001 [18], based upon the idea that it can imitate the behavior that a musician needs, a well-balanced harmony. The advantage of HS is that it has a simple model and good performance in the global search domain. Furthermore, HS has been applied in numerous real-world optimization problems [19-21]. HS steps are shown in Algorithm 1.

The first step of HS is to initialize the harmony memory size *HMS*, harmony memory consideration rate *HMCR*, maximum dimension *D*, the pitch adjusting rate *PAR* and the bandwidth *BW*.

Then, the second step is to initialize harmony memory *x*, as in (2):

$$x_{i,j} = x_{j,L} + rand.(x_{j,U} - x_{j,L}),$$
 (2)

where  $x_{j,L}$  and  $x_{j,U}$  are lower bounds for a decision variable. In step 3, check the memory consideration of HS. If  $R_1$  is smaller than *HMCR*, execute as in (3):

$$x_{new,j=} x_{r,j} (r \in 1,2,3, \dots HMS),$$
 (3)

where  $x_{r,j}$  is the index random of the harmony memory for one dimension,  $r \in \{1, 2, 3, ..., HMS \text{ and } j \in \{1, 2, 3, ..., D\}$ , while *D* is the maximum number of dimensions.

After that, check the pitch adjustment condition; if  $R_2$  is smaller than *PAR* and  $R_3$  is smaller than 0.5, execute as in (4):

$$x_{new,j} = x_{new,j} + \varphi \times BW , \qquad (4)$$

where  $\varphi$  is a random number uniformly distributed in the range [-1,1] and *BW* is a constant value. If  $R_3$  is larger than 0.5, execute as in (5):

$$x_{new,j} = x_{new,j} - \varphi \times BW.$$
(5)

If R, is larger than HMCR, follow (6):

$$x_{new,j} = x_{j,L} + rand.(x_{j,U} - x_{j,L}),$$
 (6)

where *rand* is a random number uniformly distributed in the range [0,1].

In step 4, if  $f(x_{new})$ , which is an objective function of the new harmony memory  $x_{new'}$  is smaller than  $f(x_{worst})$ , which is an objective function of the worst harmony memory  $x_{worst'}$  execute as in (7):

$$x_{worst} = x_{new}.$$
 (7)

#### Algorithm 1: HS

**Input:** Harmony memory size *HMS*, harmony memory consideration rate, *HMCR* maximum dimension *D*, maximum generation *G*, pitch adjusting rate, *PAR* and bandwidth, *BW* 

**Output:** worst harmony,  $x_{worst'}$  function objective of worst harmony  $f(x_{worst})$ 

**Step 1:** Initialize HMS, HMCR, PAR, D, G, and PAR.

Step 2: Initialize harmony memory HM as below:

For i=1 to *HMS* do For j=1 to *D* Execute as in (2). End For Calculate  $f(x_i)$ End For

**Step 3:** Improvise g=0, while the stopping criterion is inadequate (g < G) do

For j=1 to D do If  $R_1 \le HMCR$ % memory consideration Execute as in (3).

% pitch adjustment If  $R_2 \le PAR$  then

```
If R_3 \le 0.5
Execute as in (4).
Else
Execute as in (5).
End If
End If
Else
% random selection
Execute as in (6).
End If
End For
```

# Step 4: Update the worst harmony.

Select the worst harmony vector  $x_{worst}$  in the current harmony memory and calculate  $f(x_{now})$  and  $f(x_{worst})$ 

If  $f(x_{new}) \le f(x_{worst})$ Execute as in (7). End If g=g+1; End While

**Step 5:** Algorithm stops when the best solution is obtained.

# 3.2. PATCH-LEVY BEES ALGORITHM (PLBA)

The PLBA algorithm was proposed by Wasim et al. in 2016 [16]. During initialization, local search and global search of the PLBA, a patch concept and the Levy distribution were modeled. Using patch with the PLBA helps us distribute solutions in the search space, while the Levy distribution is used to get the benefit of its concept and step size. Levy distribution step size usually comprises several short steps followed by occasional longer jumps. Short steps make the exploitation of the most promising area on which the majority of the population is focused. However, a rarely long jump keeps exploring the search space by part of the population. Generally, patch and levy flights make the PLBA track more than one pick in terms of the maximization problem. Using a suitable step size of levy flights in initialization and global search, the PLBA maintained the diversity of the solution because of the rarely long jump.

The PLBA is attested to select accurate thresholds for image segmentation [16]. In comparison to Kapur's objective functions, Otsu's show a better segmentation result.

The PLBA solution represents a combination of r thresholds. Hence, the bee solution can be represented as in (8).

$$bee = (t_1, t_2, ..., t_r)^T$$
, (8)

where  $t_1 \in [0, L_1]$  and  $t_i < t_{i+1}$  for all  $t \in [1, r]$ .

The PLBA-based algorithm steps are shown in Algorithm 2. Generally, initializing the threshold values is done with levy step  $\gamma = \gamma_1$  as in (9), while in global search the levy step  $\gamma = \gamma_3$ . Local search is performed as in (10).

$$t_i = c_j + (2r - 1) \times Levy(\gamma) ,i = 1, 2, ..., n; j = 1, 2, ..., P,$$
(9)

where  $c_j$  is the center of the  $j^{th}$  patch,  $r \in uniform(0,1)$ , and gives the direction to the flight.

$$t_i = t_{bestcur} + (2r - 1) \times Levy(\gamma_2),$$
  

$$i = 1, 2, \dots, nep \text{ (or } nsp\text{)}.$$
(10)

## 3.3. OTSU'S CRITERION

Otsu's thresholding is a well-known method in image segmentation. It is used to choose optimal thresholding by maximizing the variance between different classes and minimizing it within the same class.

Let *h* be the gray-level histogram of an image with *L* gray levels and *N* pixels. So h(i) is the number of gray levels *i*,  $i \in [0,L]$  in the image. Then, the probability of gray level *i* in the image can be calculated as in (11).

## Algorithm 2: PLBA

**Input:** Number of thresholds (r), number of iterations (s), number of scout bees (n), number of selected sites (m), number of elite sites (e), Number of recruited bees for each site of the e sites, (nsp), number of bees recruited for every site of the remaining, (m-e) sites, (nsp), Step size of Levy flights ( $\gamma_1$ ), Step size of Levy flights ( $\gamma_3$ )

**Output:** Optimal threshold values (t<sub>1</sub>,t<sub>2</sub>,...,t<sub>r</sub>)

**Step 1:** Initialize each scout bees as in (8); with a combination of threshold values defined as in (9)

**Step 2:** Evaluate the fitness of each combination of thresholds as in (18) for the PLBA-Otsu algorithm.

**Step 3:** Repeat for s or until a given stopping criterion is met

**3.1**: Select the best m; where m<n; combinations of thresholds from the population

**3.2**: Select the best e ; where e<m; combinations of thresholds from the population

**3.3**: Start local search around the best *m* combinations by generating more combinations of thresholds (*nep*) around *e* combinations and (*nsp*) threshold combinations generated around the remaining *m-e* combinations. Each combination of thresholds ( $t_i$ ) is represented as in (8) and generated as in (10),

where  $t_{bestcur}$  is the current best combination of thresholds in the neighborhood,

**3.4**: Start global search by redistributing the remaining *n*-*m* bees by creating a new solution represented as in (8) and (9)

**3.5**: Evaluate the fitness of each combination of the *n*-*m* combinations as in (18).

**3.6**: Choose the best threshold combination of local and global search

**Step 4:** A combination of thresholds with the best fitness value is chosen to represent the optimal thresholds.

$$P_i = \frac{h(i)}{N}, P_i \ge 0, \sum_{i=1}^{L-1} P_i = 1.$$
 (11)

Otsu [9] introduced three discriminant criteria based on discriminate analysis to measure separation as in (12).

$$\lambda = \frac{\sigma_B^2}{\sigma_W^2} , k = \frac{\sigma_T^2}{\sigma_W^2} , n = \frac{\sigma_B^2}{\sigma_T^2} , \qquad (12)$$

where  $\sigma_{B}^{2}$  is the variance between classes,  $\sigma_{W}^{2}$  is the variance within class and  $\sigma_{T}^{2}$  is the total variance of gray levels.

In bi-level thresholding, Otsu divided the image into two classes, i.e. the first class  $C_1$  with pixels in the range [0,*t*-1], and the second class  $C_2$  with pixels in the range [t,*L*-1] by threshold *t*. The between class variance is calculated as in (13).

$$\sigma_B^2(t) = w(0,t) (\mu(0,t) - \mu(0,L))^2 + w(t,L) (\mu(t,L) - \mu(0,L))^2,$$
(13)

where  $w(0,t) = \sum_{i=0}^{t-1} p_i$  is the weight of the first class  $C_1, w(t,L) = \sum_{i=t}^{L-1} p_i$  is the weight of the second class  $C_2$  and w(0,t) + w(t,L) = 1.

The mean of the first and second classes is given as in (14) and (15).

$$\mu(0,t) = \sum_{i=0}^{t-1} \frac{ip_i}{w(0,t)},\tag{14}$$

$$\mu(t,L) = \sum_{i=t}^{L-1} \frac{ip_i}{w(t,L)} \,. \tag{15}$$

The total mean level of the original image is defined as in (16).

$$\mu(0,L) = w(0,t)\mu(0,t) + w(t,L)\mu(t,L).$$
(16)

Otsu's thresholding method selects the optimal thresholds t<sup>\*</sup> by maximizing the between class variance of (12) as follows (17):

$$t^* = \operatorname{argmax}\{\sigma_B^2\}.$$
 (17)

Assuming *r* thresholds were supposed to be chosen, two dummy thresholds  $t_0=0$  and  $t_r+1=0$  are used for computational convenience, and the objective function becomes as in (18):

$$\sigma_B^2(t_1, t_2, \dots, t_r) = \sum_{i=0}^c w(t_1, t_{i+1})(\mu(t_1, t_{i+1}) - \mu(0, L))^2.$$
(18)

## 4. EXPERIMENTAL SETUP

#### 4.1. TEST IMAGE

The MRI data for this research collected from the Hospital Counselor Tunku Muhriz (HCTM) with a sample T2 weighted of 9 axial plane brain images for 2 patients represented as Patient A and Patient B are shown in Table 1. Patient A is a 40-year old Malay male and Patient B is a 48-year old Malay female. T2-weighted images in JPEG format show water brighter and fat darker. The details of each image are shown in Table 1 and the images with their histograms are shown in Fig. 1.

 Table 1. Details of brain MRI images

 collected from HCTM

Test Image	Brain Tumor Type	Number of Patient Data	Spatial Resolution
Slice 9		Patient A	1494x1780
Slice 162		Patient A	1170x1344
Slice 164		Patient A	1170x1344
Slice 165	Intraventricular Tumor with	Patient A	1170x1344
Slice 166	Epidermoid cyst	Patient A	1170x1344
Slice 167		Patient A	1170x1344
Slice 168		Patient A	1170x1344
Slice 169		Patient A	1170x1344
Slice 38	Small Falx Meningioma with Arachnoid Cyst	Patient B	1024x1024

## 4.2. PERFORMANCE EVALUATION

#### A. Uniformity

Uniformity measured was employed to compare optimization technique performance [22]. The misclassification error is calculated by (19):

$$U = 1 - 2 * c * \frac{\sum_{j=0}^{c} \sum_{i \in R_j} (f_i - \mu_j)^2}{N * (f_{max} - f_{min})^2},$$
(19)

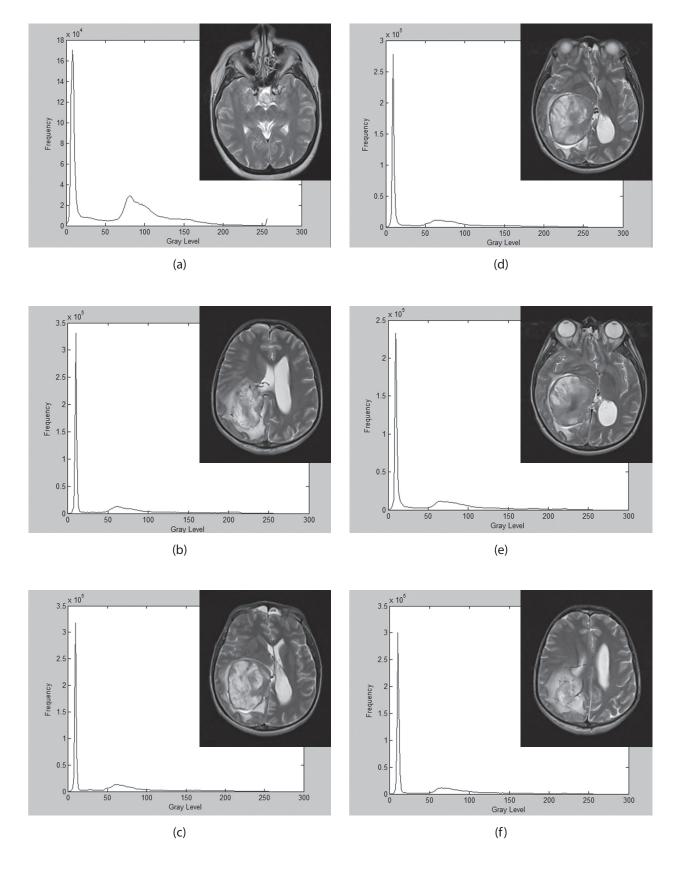
where *c* is the number of thresholds used to segment the image.  $R_j$  is the *jth* segmented region and  $f_i$  is the intensity level of pixels for the segmented region.  $\mu_j$  is the mean of the *jth* segmented image and *N* is a total of pixels in the image. Maximum and minimum intensity of an image are represented as  $f_{max} - f_{min}$ , respectively. Generally, misclassification errors may lie between 0 and 1.

The performance of the algorithm is better when the misclassification error is high.

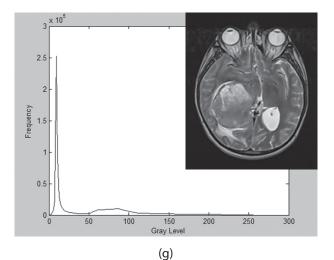
Thus, the uniformity is an indication of better image quality when U=1, and of worse image quality when U=0.

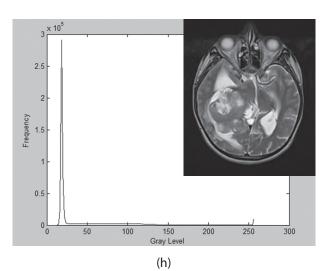
# **B. Stability**

If the performance in each run is not unique, it is evaluated by more than one run. Each run obtained different initial values. The robustness of the algorithm is based on the acceptance of its outcome. Therefore, the algorithm was run for 50 times. The stability of the algorithm evaluated was based on the average of the mean and standard deviation for all runs. If each run hardly varies from one to another, the algorithm was considered to be stable. The mean and standard deviation are demonstrated as in (20) and (21).



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where  $\mu_j$  is the objective function value or the fitness value at the *jth* run and *N* is the number of run.

#### C. Structural Similarity Index (SSIM)

SSIM measures the similarity between the original image and the thresholded image, and it is expressed as follows:

$$SSIM = \frac{(2\mu_i\mu_i + C1)(2\sigma_{ii} + C2)}{(\mu_i^2 + \mu_i^2 - C1)(\sigma_I^2 + \sigma_I^2 - C2)},$$
(22)

$$\sigma_{ii} = \frac{1}{N-1} \sum_{i=1}^{N} (I_i - \mu_I) (\tilde{I}_i - \mu_{\tilde{I}}),$$
(23)

where  $\mu_{I}$  and  $\mu_{\tilde{I}}$  are the mean values of the original image *I* and the reconstructed image  $\tilde{I}$ , and  $\sigma_{\tilde{I}}$  is the standard deviation of the original image *I* and the reconstructed image  $\tilde{I}$ ,  $\sigma_{\tilde{I}}$  is the cross-correlation and C1 and C2 are constants equal to 0.065. The SSIM ranges between -and +1 and the SSIM value is equal to one. This shows that the original image and the reconstructed image (a threshold image) are similar. It is presumed that the algorithm can produce acceptable p performance if the SSIM value is close to 1.

#### D. Peak Signal-to-Noise Ratio (PSNR)

The PSNR, which is quantified in decibels (dB), shows a dissimilarity between an input image and a threshold image. A higher value of the PSNR requires better quality of the threshold image. RMSE and the PSNR values are calculated as follows:

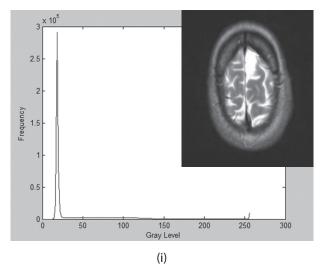
$$RMSE = \sqrt{\frac{1}{MN} \sum_{I}^{M} \sum_{J}^{N} \left[ f(I, J) \tilde{f}(I, J) \right]^{2}}, \qquad (24)$$

$$PSNR = 20\log_{10}\left(\frac{255}{RMSE}\right),$$
 (25)

where  $M \times N$  is the size of an image, while *I* and *J* represent the pixel values of the original and decompressed images, respectively. In this experiment, researchers have taken  $M \times N$  to be a square image. f(I,j) is an original image, whereas  $\tilde{f}(I,j)$  is a reconstructed image.

## 4.3. PARAMETER SETTINGS

For PLBA-Otsu and HS-Otsu tests presented in this paper, the default parameters of all methods are listed in tables 2 and 3, respectively. The PLBA-Otsu parameter values were suggested by Wasim et al. in 2016 [16]. The Levy step size in local search ( $Y_1$ ) was set to a small value to support the exploitation capability of good regions, while the Levy step size in global search and initialization ( $Y_2$  and  $Y_3$ ) was set to large values to maintain the diversity of the population [16]. Basically, HS parameters are the harmony memory size (HMS), that is, the number of solution vectors lying on the harmony memory (HM), the harmony memory consideration



**Fig. 1.** Original image and the grayscale histogram of an image

mean (
$$\sigma$$
) =  $\frac{1}{N} \sum_{j}^{N} \mu_{j}$ , (20)

standard deviation = 
$$\sum_{j=1}^{N} (\mu_{j-}\sigma)^2$$
, (21)

rate (HMCR), the pitch adjusting rate (PAR), the distance bandwidth (BW), and the number of improvisations (NI), which represents the total number of iterations. These HS parameters, with the exception of NI, were obtained from Oliva et al. [20]. HS is stopped when the NI maximum is reached. The one-way ANOVA test is the most suitable statistical test for comparing two algorithms during performance evaluation. Table 6 presents the one-way ANO-VA test results regarding the objective value obtained from Table 4.

#### Table 4. Objective value

#### Table 2. Parameters used for the PLBA method

Parameter	Value
Number of scout bees, (n)	26
Number of selected sites (patches), (m)	18
Number of elite sites (patches), (e)	9
Number of recruited bees for each site of e sites, (nep)	25
Number of bees recruited for every site of the remaining ( <i>m-e</i> ) sites, ( <i>nsp</i> )	21
Step size of Levy flights (local), $(Y_{1_{init}})$	0.01
Step size of Levy flights (initial), $(Y_2)$	0.5
Step size of Levy flights (global), $(\gamma_3)$	0.5

#### **Table 3.** Parameters used for the HS method

Parameter	Value
Harmony Memory Consideration Rate, (HMCR)	0.75
Harmony Memory Size (HMS)	100
Pitch Adjusting Rate (PAR)	0.5
Bandwidth (bw)	0.5
Number of Improvisations (NI)	100

### 4.4. EXPERIMENTAL ENVIRONMENT

Both PLBA and HS based multilevel thresholding were implemented in the Matlab Language under operation system Microsoft 10 Pro. HS used the platform of Intel (R) Core<sup>™</sup> i7-2620M CPU @ 2.70 GHz 2.70 GHz and 4.00 GB RAM. On the other hand, the PLBA used the platform of Intel (R) Core<sup>™</sup> i7-2640M CPU @ 2.80 GHz 2.80 GHz and 8.00 GB RAM.

# 5. RESULTS AND DISCUSSION

# 5.1. SOLUTION QUALITY

The mean values of Otsu's objective functions and PLBA and HS optimal thresholds are shown in Table 4 and Table 5, respectively.

PLBA and HS algorithms yield different solution quality (thresholds). In Table 4, it can be observed that the PLBA algorithms provide higher objective values than HS for Otsu's criteria in relation to all numbers of thresholds. It is triggered by the balance of PLBA search through its exploitation and exploration.

An example of segmented images and corresponding thresholds on the histogram obtained by means of PLBA and HS algorithms at threshold levels 2, 3, 4 and 5 are shown in Fig 2. In these figures, it can be observed that a segmented image has high performance when (C=5), compared with (C=4), (C=3) and (C=2).

Fest imagesHSPLBA22758.60352763.705232860.92832868.584042917.82252931.563052954.82622972.793662954.82622972.793662622.73532626.323162732.77602741.092362769.87602803.770472623.05312627.640462764.93662766.9936722623.05312627.6404722623.05312676.993662776.45262766.99362764.9936722565.05332570.0430722565.05332570.043082666.89962673.99242748.9369922565.72742569.4757922565.72742569.4757922565.72742569.4759922565.72742569.4759922565.72742569.4759922565.72742569.4759102229222922211192212222132221422215222162221722218222192221922<			Objectiv	Objective value			
Slice 932860.92832868.584042917.82252931.563052954.82622972.793652954.82622972.793642622.73532626.323142771.13172783.922842771.13172783.922852789.87602803.770462764.5262669.93662776.45262766.993662774.87612788.345972565.05332570.043072565.05332570.043062734.91812724.594972565.72742669.7392462734.91812748.936972565.72742669.475782667.60622676.299462730.95212742.930172420.40712423.180982509.18112517.179742549.36272561.390472569.72992580.887292569.72992580.887292569.72992580.887292677.91382687.071112724.54602736.663712727.287032614.336412724.54602756.893722608.39552614.336412720.63852614.336422766.3959260.541422608.39552614.336422766.3959260.541422766.3959260.541432720.63852614.33642276.3539260.5414 </th <th>Test images</th> <th>c</th> <th></th> <th></th>	Test images	c					
Slice 9         4         2917.8225         2931.5630           5         2954.8262         2972.7936           5         2622.7353         2626.3231           4         2732.7760         2741.0923           4         2771.1317         2783.9228           5         2789.8760         2803.7704           6         2789.8760         2803.7704           7         262.30531         2627.936           6         2764.936         2756.4526           7         2764.936         2766.9936           5         2774.8761         2788.3459           6         2774.8761         2788.3459           6         2774.8761         2788.3459           7         2565.0533         2570.0430           7         2744.911         2748.9369           6         2734.9181         2748.9369           5         2734.9181         2748.9369           6         2760.9167         2723.494           7         2565.7274         2569.4757           8         2667.6062         2676.2994           8         2670.9167         2723.494           9         2600.9167         2742.9301		2	2758.6035	2763.7052			
42917.82252931.563052954.82622972.793662622.73532626.323162732.7602741.092342771.13172783.922852789.87602803.770462623.05312627.760462766.45262766.993672783.79242756.452662774.87612783.459172766.95362673.992462766.99362673.992472783.91812748.936962734.91812748.936972734.91812748.936972730.95212742.930172730.95212742.930172730.95212742.930172569.72992580.887282677.91382687.07716267.91382687.07717272.454602736.663792741.90342757.2897282741.90342757.2897292683.9552614.336472745.059280.541472720.63852614.336482720.63852614.336492766.50792776.893792608.39552614.336492766.50792776.8937202780.359280.5414211886.39681838.518922288.69532614.3364232780.5359280.5414242764.50792776.8937252780.5359280.5414<		3	2860.9283	2868.5840			
22622.73532626.323132732.77602741.092342771.13172783.922852789.87602803.770442764.5262667.604352774.87612788.345962774.87612788.345962774.87612788.345962774.87612788.345972666.89962673.992462734.91812724.594972666.760622676.293472734.91812748.936972734.91812742.930172565.72742569.475782667.60622676.293492565.72742569.475792667.60622676.293492565.72742569.475792667.60622676.293492730.95212742.930192569.72992580.887292569.72992580.887292569.72992580.887292569.72992580.887292569.72992580.887292677.91382687.077192774.93042757.289792608.39552614.336492741.90342759.82849276.50592800.541492785.03592800.541492785.03592800.541492785.03592800.541492785.03592800.541492785.03592800.541492785.03592800.5414 <td rowspan="2">Slice 9</td> <td>4</td> <td>2917.8225</td> <td>2931.5630</td>	Slice 9	4	2917.8225	2931.5630			
Slice 1623 42732.77602741.092342771.13172783.922852789.87602803.770462623.05312627.7604732716.43482725.457262776.45262766.993672774.87612788.3459722565.00532570.0430722565.00532570.0430722565.00532570.0430722565.72742569.4757722565.72742569.4757722565.72742569.4757722565.72742569.4757722565.72742569.4757722565.72742569.4757722565.72742569.4757722730.95212742.9301722509.18112517.1797722569.72992580.8872722569.72992580.8872722569.72992580.8872732677.91382687.0711722584.48922588.6853722584.48922588.6853722272227222722282229222922292229222		5	2954.8262	2972.7936			
Slice 162         4         2771.1317         2783.9228           5         2789.8760         2803.7704           6         2623.0531         2627.7604           3         2716.4348         2725.4572           4         2756.4526         2766.9936           5         2774.8761         2788.3459           5         2774.8761         2788.3459           6         2756.053         2570.0430           7         2565.0053         2570.0430           6         2734.9181         2748.9369           6         2734.9181         2748.9369           5         2734.9181         2748.9369           6         2767.09521         2667.602           6         2709.1167         2722.3494           7         2420.4071         2423.1809           6         2569.7294         2561.3904           7         2569.7299         2580.8872           7         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2569.7299         2580.8872           7         2569.7299         2580.8872           8         2677.9138         2687.0771		2	2622.7353	2626.3231			
42771.13172783.922852789.87602803.770452762.305312627.760432716.43482725.457242756.45262766.993652774.87612788.345962750.04302788.3459722565.00532570.0430732666.89962673.992442711.11942724.594952734.91812748.936962734.91812748.9369722565.72742569.475732667.60622676.299442709.11672722.349452730.95212742.930162509.18112517.1797722569.72992580.8872732667.91382667.01482677.91382667.071142549.36272568.8853932677.91382667.071162734.90342736.6637732677.91382667.071382724.54602736.6637932677.91382667.071392608.39552614.336492764.50792776.89379280.54142764.50792776.89379280.54142764.50792776.893752785.0359280.5414280.541410216.83061838.5189280.541411216.83071922.6860260.5414		3	2732.7760	2741.0923			
2         2623.0531         2627.7604           3         2716.4348         2725.4572           4         2756.4526         2766.9936           5         2774.8761         2788.3459           6         2774.8761         2788.3459           7         2565.0053         2570.0430           7         2565.0053         2673.9924           6         2711.1194         2724.5949           5         2734.9181         2748.9369           5         2734.9181         2748.9369           6         2791.1194         2724.5949           5         2734.9181         2748.9369           6         2709.1167         2722.3494           6         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2730.9521         2742.9301           7         2         2420.4071         2423.1809           8         2509.1811         2517.1797           4         2549.3627         2580.8872           5         2569.7299         2580.8872           5         2741.9034         2757.2897           6         2774.5460         2736.6637	Slice 162	4	2771.1317	2783.9228			
Slice 16432716.43482725.457242756.45262766.993652774.87612788.345922565.00532570.043032666.89962673.992442711.11942724.594952734.91812748.936962734.91812748.936972565.72742569.475732667.60622676.299442709.11672722.349452730.95212742.930162730.95212742.930172423.18092420.407122569.72992580.887262569.72992580.887252569.72992580.887252569.72992580.887252677.91382687.077142724.54602736.663752741.90342757.289752706.33552614.336462730.63852729.828472608.39552614.336482720.63852729.828462730.63852729.82847276.503592800.541462785.03592800.541471836.39681838.518981916.83071922.6860		5	2789.8760	2803.7704			
Slice 164         4         2756.4526         2766.9936           5         2774.8761         2788.3459           2         2565.0053         2570.0430           3         2666.8996         2673.9924           4         2711.1194         2724.5949           5         2734.9181         2748.9369           5         2734.9181         2748.9369           6         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2730.9521         2742.9301           7         2420.4071         2423.1809           6         2509.1811         2517.1797           7         2569.7299         2580.8872           5         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2569.7299         2580.8872           8         2677.9138         2687.0771           9         2608.3955         2614.3364           9         2720.6385         279.8284           9         2726.5079         276.8937     <		2	2623.0531	2627.7604			
4         2756.4526         2766.9936           5         2774.8761         2788.3459           2         2565.0053         2570.0430           3         2666.8996         2673.9924           4         2711.1194         2724.5949           5         2734.9181         2748.9369           6         2734.9181         2748.9369           6         2709.1167         2722.3494           6         2709.1167         2722.3494           5         2730.9521         2742.9301           5         2730.9521         2742.9301           6         2709.1167         2423.1809           7         2569.7299         2580.8872           6         2509.1811         2517.1797           7         2569.7299         2580.8872           7         2569.7299         2580.8872           8         2677.9138         2687.0771           8         2677.9138         2687.0771           9         2608.3955         2614.3364           9         2720.6385         2614.3364           9         2720.6385         2729.8284           9         2726.5359         2800.5414 <td< td=""><td></td><td>3</td><td>2716.4348</td><td>2725.4572</td></td<>		3	2716.4348	2725.4572			
2         2565.0053         2570.0430           3         2666.8996         2673.9924           4         2711.1194         2724.5949           5         2734.9181         2748.9369           6         2709.1167         2569.4757           7         2667.6062         2676.2994           4         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2730.9521         2742.9301           7         2569.7294         2561.3904           6         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2677.9138         2687.0771           6         2741.9034         2757.2897           5         2741.9034         2757.2897           5         2760.6385         2614.3364           6         2720.6385         2614.3364           6         2764.5079         2776.8937           5         2785.0359         2800.5414 <td< td=""><td>Slice 164</td><td>4</td><td>2756.4526</td><td>2766.9936</td></td<>	Slice 164	4	2756.4526	2766.9936			
Slice 16532666.89962673.992442711.11942724.594952734.91812748.936962755.72742569.475732667.60622676.299442709.11672722.349452730.95212742.930162730.95212423.180972423.18092423.180982509.18112517.179742549.36272561.390452569.72992580.887262569.72992580.8872722584.48922588.685332677.91382687.077142724.54602736.663752741.90342757.289762706.38552614.336472608.39552614.336482720.63852729.828442764.50792776.893752785.03592800.541462785.03592800.5414721836.396881916.83071922.6860		5	2774.8761	2788.3459			
Slice 165         4         2711.1194         2724.5949           5         2734.9181         2748.9369           5         2756.7274         2569.4757           6         2667.6062         2676.2994           6         2709.1167         2722.3494           6         2709.0521         2742.9301           7         2420.4071         2423.1809           6         2509.1811         2517.1797           7         2420.4071         2423.1809           7         2420.4071         2423.1809           7         2420.4071         2423.1809           7         2420.4071         2423.1809           7         2420.4071         2433.1809           8         2509.1811         2517.1797           4         2549.3627         2560.3904           5         2569.7299         2580.8872           6         2677.9138         2687.0771           8         2677.9138         2687.0771           9         270.6385         279.8284           9         270.6385         2729.8284           9         2764.5079         2776.8937           5         2785.0359         2800.5414 </td <td></td> <td>2</td> <td>2565.0053</td> <td>2570.0430</td>		2	2565.0053	2570.0430			
4         2711.1194         2724.5949           5         2734.9181         2748.9369           5         2734.9181         2748.9369           6         2565.7274         2569.4757           3         2667.6062         2676.2994           4         2709.1167         2722.3494           5         2730.9521         2742.9301           5         2730.9521         2742.9301           6         2730.9521         2423.1809           7         2420.4071         2423.1809           6         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           5         2569.7299         2580.8872           6         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2720.6385         2614.3364           6         2720.6385         2729.8284           7         2608.3955         2614.3364           6         2785.0359         2800.5414 <td< td=""><td></td><td>3</td><td>2666.8996</td><td>2673.9924</td></td<>		3	2666.8996	2673.9924			
2         2565.7274         2569.4757           3         2667.6062         2676.2994           4         2709.1167         2722.3494           5         2730.9521         2742.9301           5         2730.9521         2423.1809           6         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           5         2569.7299         2580.8872           6         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2580.8872         2580.8872           6         2677.9138         2687.0771           6         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2720.6385         2614.3364           6         2720.6385         2729.8284           7         2608.3955         2614.3364           6         2764.5079         2776.8937           5         2785.0359         2800.5414           6         2785.0359         2800.5414 <td< td=""><td>Slice 165</td><td>4</td><td>2711.1194</td><td>2724.5949</td></td<>	Slice 165	4	2711.1194	2724.5949			
Slice 166         3         2667.6062         2676.2994           4         2709.1167         2722.3494           5         2730.9521         2742.9301           6         2730.9521         2742.9301           7         2420.4071         2423.1809           8         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2584.4892         2588.6853           7         2569.7299         2580.8872           8         2677.9138         2687.0771           9         2580.8872         2588.6853           5         2741.9034         2757.2897           5         2706.385         2729.8284           6         2706.385         2729.8284           6         2764.5079         2776.8937           5         2785.0359         2800.5414           6         2785.0359         2800.5414           6         2785.0359         2800.5414           7         1836.3968         1838.5189           8         1916.8307         1922.6860     <		5	2734.9181	2748.9369			
Slice 166         4         2709.1167         2722.3494           5         2730.9521         2742.9301           5         2730.9521         2742.9301           6         2420.4071         2423.1809           7         2420.4071         2423.1809           8         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2584.4892         2588.6853           6         2677.9138         2687.0771           8         2677.9138         2687.0771           9         2741.9034         2757.2897           5         2741.9034         2757.2897           6         2720.6385         2614.3364           9         2706.3855         2614.3364           6         2720.6385         2729.8284           6         2785.0359         2800.5414           7         280.5314         2785.0359           5         2785.0359         2800.5414           6         2785.0359         2800.5414           7         1836.3968         1838.5189		2	2565.7274	2569.4757			
4         2709.1167         2722.3494           5         2730.9521         2742.9301           5         2730.9521         2423.1809           2         2420.4071         2423.1809           3         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2584.4892         2588.6853           6         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2720.6385         2614.3364           6         2720.6385         2729.8284           7         2608.3955         2614.3364           8         2720.6385         2729.8284           6         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860		3	2667.6062	2676.2994			
2         2420.4071         2423.1809           3         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           7         2584.4892         2588.6853           8         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           5         270.6385         2614.3364           63         2720.6385         2729.8284           64         2726.385         2729.8284           7         2608.3955         2614.3364           9         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860	Slice 166	4	2709.1167	2722.3494			
3         2509.1811         2517.1797           4         2549.3627         2561.3904           5         2569.7299         2580.8872           6         2569.7299         2580.8872           8         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           5         2706.3855         2614.3364           63         2720.6385         2729.8284           63         2764.5079         2776.8937           5         2785.0359         2800.5414           65         2785.0359         2800.5414           63         1916.8307         1922.6860		5	2730.9521	2742.9301			
Slice 167         4         2549.3627         2561.3904           5         2569.7299         2580.8872           5         2569.7299         2580.8872           6         2584.4892         2588.6853           6         2677.9138         2687.0771           6         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2720.6385         2614.3364           6         2720.6385         2729.8284           6         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860		2	2420.4071	2423.1809			
4         2549.3627         2561.3904           5         2569.7299         2580.8872           2         2584.4892         2588.6853           3         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           5         270.6385         2614.3364           6         2720.6385         2729.8284           7         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860		3	2509.1811	2517.1797			
2         2584.4892         2588.6853           3         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2608.3955         2614.3364           7         2608.3955         2614.3364           8         2720.6385         2729.8284           4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860	Slice 167	4	2549.3627	2561.3904			
3         2677.9138         2687.0771           4         2724.5460         2736.6637           5         2741.9034         2757.2897           6         2706.83955         2614.3364           7         2608.3955         2614.3364           8         2720.6385         2729.8284           3         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860		5	2569.7299	2580.8872			
Slice 168         4         2724.5460         2736.6637           5         2741.9034         2757.2897           5         270.6385         2614.3364           3         2720.6385         2729.8284           4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           Slice 38         3         1916.8307         1922.6860		2	2584.4892	2588.6853			
4         2724.5460         2736.6637           5         2741.9034         2757.2897           2         2608.3955         2614.3364           3         2720.6385         2729.8284           4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           Slice 38         3         1916.8307         1922.6860		3	2677.9138	2687.0771			
2         2608.3955         2614.3364           3         2720.6385         2729.8284           4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           Slice 38         3         1916.8307         1922.6860	Slice 168	4	2724.5460	2736.6637			
3         2720.6385         2729.8284           4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           3         1916.8307         1922.6860		5	2741.9034	2757.2897			
Slice 169 4 2764.5079 2776.8937 5 2785.0359 2800.5414 2 1836.3968 1838.5189 3 1916.8307 1922.6860		2	2608.3955	2614.3364			
4         2764.5079         2776.8937           5         2785.0359         2800.5414           2         1836.3968         1838.5189           Slice 38         3         1916.8307         1922.6860	Slice 160	3	2720.6385	2729.8284			
2 1836.3968 1838.5189 3 1916.8307 1922.6860 Slice 38	Slice 169	4	2764.5079	2776.8937			
3 1916.8307 1922.6860 Slice 38		5	2785.0359	2800.5414			
Slice 38		2	1836.3968	1838.5189			
	Slice 29	3	1916.8307	1922.6860			
4 1947.7889 1955.8094	Slice 38	4	1947.7889	1955.8094			
5 1965.1856 1974.0217		5	1965.1856	1974.0217			

The hypothesis made for the analysis of Table 6 is as follows:

**Null hypothesis, H0**: There is no significant difference in the objective value between the two methods (the PLBA and HS).

**Alternative hypothesis, H1**: There is a significant difference in the objective value between the two methods (the PLBA and HS).

## Table 5. Optimal threshold value

		Optimal threshold values				
Test images	c	HS	PLBA			
	2	48, 121	43,123			
	3	43, 96, 147	39,95,158			
Slice 9	4	43, 86, 130, 193	35,75,114,169			
	5	19, 49, 106, 141, 203	34,69,97,133,177			
	2	44, 128	43,123			
	3	44, 99, 166	39,95,158			
Slice 162	4	33, 75, 114, 168	35,75,114,169			
	5	39, 77, 104, 130, 175	34,69,97,133,177			
	2	45, 128	42,120			
	3	32, 90, 146	38,90,148			
Slice 164	4	33, 76, 118, 167	35,75,116,166			
	5	30, 62, 92, 130, 170	32,66,94,133,176			
	2	46, 122	44,121			
	3	45, 97, 149	41,96,154			
Slice 165	4	44, 96, 132, 164	36,77,118,172			
	5	32, 63, 88, 127, 181	34,71,101,139,184			
	2	47,128	46,125			
	3	41, 98, 156	42,95,154			
Slice 166	4	36, 86, 118,171	37,78,115,167			
	5	34, 76, 102, 144, 205	36,75,106,147,192			
	2	43, 124	45,122			
	3	44, 92, 162	41,94,151			
Slice 167	4	42 87, 137, 179	38,82,122,175			
	5	30, 69, 105, 156, 188	36,74,102,138,184			
	2	49, 126	46,125			
	3	44, 112, 168	42,95,154			
Slice 168	4	32, 81, 116, 167	37,78,115,167			
	5	19, 46, 77, 126, 177	36,75,106,147,192			
	2	48, 135	44,121			
Cline 100	3	46, 100, 165	41,96,154			
Slice 169	4	42, 85, 121, 157	36,77,118,172			
	5	34, 72, 108, 141, 186	34,71,101,139,184			
	2	59, 164	42,120			
Clice 20	3	49, 97, 180	38,90,148			
Slice 38	4	33, 81, 128, 196	35,75,116,166			
	5	38, 74, 98 ,145, 222	32,66,94,133,176			

# **Table 6.** One-way ANOVA test of the PLBA and HSbased on the objective value (Otsu)

Source of Variation	SS	Df	MS	F	P-value	F crit
Between Groups	1612.64	2	806.32	0.0107	0.9894	3.1296
Within Groups	5202052	69	75392.06			
Total	5203665	71				

# Table 7. Uniformity

T		Uniformity				
Test images	c	HS	PLBA			
	2	0.9819	0.9820			
	3	0.9826	0.9827			
Slice 9	4	0.9842	0.9847			
	5	0.9841	0.9873			
	2	0.9862	0.9863			
	3	0.9898	0.9901			
Slice 162	4	0.9920	0.9921			
	5	0.9924	0.9932			
	2	0.9865	0.9868			
Slice 164	3	0.9890	0.9893			
Slice 164	4	0.9908	0.9908			
	5	0.9916	0.9918			
	2	0.9855	0.9855			
Slice 165	3	0.9876	0.9879			
Slice 105	4	0.9875	0.9901			
	5	0.9908	0.9913			
	2	0.9856	0.9856			
Slice 166	3	0.9883	0.9883			
Slice 100	4	0.9896	0.9901			
	5	0.9902	0.9908			
	2	0.9874	0.9874			
Clice 167	3	0.9892	0.9898			
Slice 167	4	0.9912	0.9918			
	5	0.9914	0.9928			

	2	0.9860	0.9860
Slice 168	3	0.9872	0.9881
Slice 108	4	0.9898	0.9902
	5	0.9893	0.9910
	2	0.9844	0.9848
Slice 169	3	0.9876	0.9879
Slice 109	4	0.9886	0.9897
	5	0.9905	0.9908
	2	0.9895	0.9895
Slice 38	3	0.9918	0.9920
Silce 50	4	0.9932	0.9935
	5	0.9941	0.9946

# **Table 8.** One-way ANOVA test of the PLBA and HSbased on uniformity

Source of Variation	SS	df	MS	F	P-value	F crit
Between Groups	5.12E-06	1	5.12E-06	0.564127	0.45512	3.977779
Within Groups	0.000635	71	9.08E-06			
Total	0.00064	71				

The *p* values are greater than 0.05 (a significance level of 5%) and the F value is less than F-critical, therefore the null hypothesis cannot be rejected. Hence, it is concluded that there is no significant difference in the objective value between the PLBA and HS.

# 5.2. UNIFORMITY

A uniformity measure of the PLBA yields the highest values of HS (refer to Table 7) in all of the test images and thresholds, with the exception of two thresholds in slices 165, 166, 167, 168 and 38. The PLBA algorithm has successfully demonstrated and yielded the best quality of segmented images.

Table 8 portrays the single-factor ANOVA test results regarding the uniformity obtained from Table 7.

The hypothesis made for the analysis of Table 8 is as follows:

**Null hypothesis, H0**: There is no significant difference in the uniformity between the two methods, i.e. the PLBA and HS.

**Alternative hypothesis, H1**: There is a significant difference in the uniformity between the two methods, i.e. the PLBA and HS.

The p values are greater than 0.05 (a significance level of 5%) and the F value is less than F-critical; therefore, the null hypothesis will not be rejected. Hence, this concludes that there is no significant difference in the uniformity between the PLBA and HS.

# 5.3. STABILITY

Based on Table 10, the PLBA algorithm shows a lower standard deviation value for all image thresholds. Thus, the PLBA is more stable compared to HS.

Table 9 presents the one-way ANOVA test results regarding uniformity obtained from Table 10.

The hypothesis made for the analysis of Table 9 is as follows:

**Null hypothesis, H0**: There is no significant difference in the standard deviation between the two methods, i.e. the PLBA and HS.

**Alternative hypothesis, H1**: There is a significant difference in the standard deviation between the two methods, i.e. the PLBA and HS.

The p values are less than 0.05 (a significance level of 5%) and the F value is greater than F-critical, by virtue of which the null hypothesis is rejected. Hence, it is concluded that there is a significant difference in the standard deviation between the PLBA and HS.

**Table 9.** One-way ANOVA test of the PLBA and HSbased on standard deviation

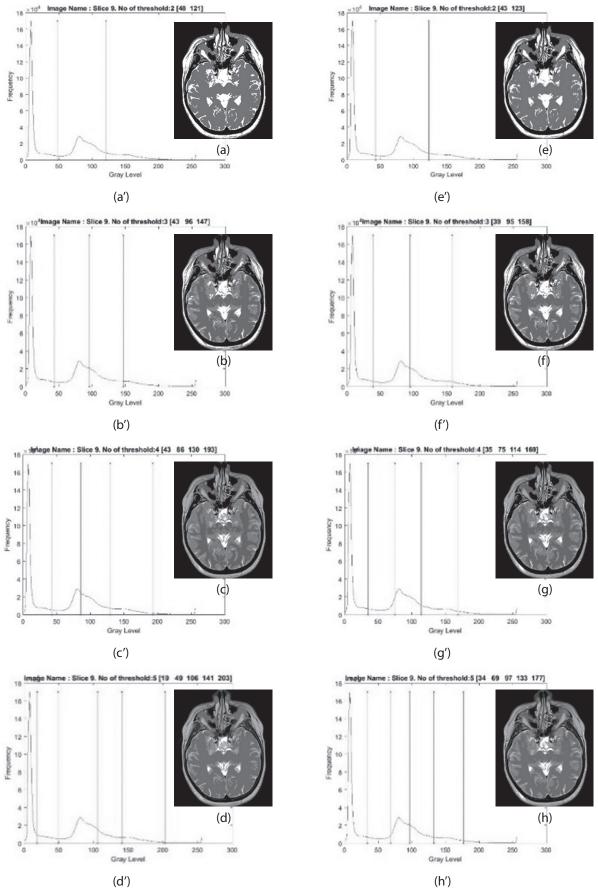
Source of Variation	SS	df	MS	F	P-value	F crit
Between Groups	5.12E-06	1	543.7303	568.3898	2.53E-35	3.977779
Within Groups	0.000635	70	0.956615			
Total	0.00064	71				

# 5.4. STRUCTURAL SIMILARITY INDEX (SSIM)

Table 11 shows that the SSIM of the PLBA is mostly higher than HS. Some SSIM of HS is higher than the PLBA, such as slices 166, 168 and 38 for c=3, and slices 167 and 169 for c=2.

# 5.5. PEAK SIGNAL-TO-NOISE RATIO (PSNR)

The results of the PSNR value in all images (refer to Table 11) are directly proportional to the increasing threshold values even though HS has achieved a higher PSNR value for most images and thresholds. The PSNR value of the PLBA is the best value in c=5 for slices 9, 162, 164 and 165. Thus, well segmented images provide a better result when the level of thresholds is high.



**Fig. 2.** Segmented images and histograms with the threshold of the Slice 9 image. (a)-(d) are the segmented images of HS for c=2,3,4,5, respectively. (a')-(d') give histograms with thresholds of HS for c=2,3,4,5, respectively. (e)-(h) show segmented images of the PLBA for c=2,3,4,5, respectively. (e')-(h') are histograms with thresholds of the PLBA for c=2,3,4,5, respectively. (e')-(h') are

# Table 10. Standard deviation

# Table 11. SSIM and PSNR

imagecHSPLBAimagecHSPLBAHSPLBA35.48E+001.48E+1245.58E+001.38E+1245.58E+001.38E+1256.38E+001.38E+1256.38E+001.38E+1246.36E+009.19E+1346.36E+009.19E+1355.74E+001.38E+1255.74E+001.38E+1272.455E+001.38E+1272.455E+001.38E+1286.66E+002.76E+1246.66E+002.76E+1255.78E+002.30E+1260.99550.99560.270572.495E+002.30E+1255.78E+002.30E+1260.99550.99560.270572.495E+002.30E+1260.99550.99560.270570.99560.99560.270580.99560.99560.270580.99560.99560.270590.99570.99580.9956101.48E+120.99580.995120.99560.99510.2716111.38E+121.38E+1250.99560.99570.261260.99570.2514111.48E+12120.99580.99510.2710130.99570.99580.2710140.99590.99580.2710150.9956<	Test	Standard deviation		Test		SSIM PSNR				
Sine 03.67E-12 45.8E+001.38E-126.8E+03.67E-12 68He 930.9960.99670.51110.465056.38E+001.38E-1250.99700.99710.88920.45230.99510.995		c	HS	PLBA		c	HS	PLBA	HS	PLBA
Siles45.55£+001.38E+1250.99730.99712.688922.6452836.38E+001.38E+1250.99730.99712.688922.6452840.575E+001.38E+1240.99600.99521.84581.8033655.75E+001.38E+1250.99640.99002.52192.5252265.75E+001.38E+1250.99640.99002.52192.5252773.58E+001.38E+1250.99640.99022.01062.205086.53E+002.76E+1260.99610.99522.03062.205050.57E+002.76E+1260.99510.99512.217052.2030880.516E+002.76E+12720.99380.99421.840202.30880.516E+001.84E+12730.99450.99482.307572.3131891.38E+12730.99450.99450.99452.77052.578191.38E+12755.58E+001.84E+1276.99510.99152.57112.573191.38E+1271.38E+1271.38E+12<		2	5.44E+00	1.84E-12		2	0.9965	0.9966	15.4965	16.0045
45,59E+001,38E+1240,9960,9972,5112,4652056,38E+001,38E+1250,99730,9972,68922,6453846,36E+009,19E+1380,99560,99522,825822,55855,74E+001,38E+1250,99640,99642,00122,558266,68E+002,76E+1280,99510,99510,99522,2630886,68E+002,76E+1280,99510,99550,99522,2630855,89E+002,76E+1280,99510,99550,99552,27022,2630855,89E+002,76E+1280,99510,99510,99512,21032,2630855,88E+001,84E+1280,99510,99510,21052,273182,4033655,88E+001,84E+1280,99510,99512,274132,403377,56E+001,84E+1280,99510,99512,274132,403385,19E+001,84E+1280,99510,99512,274132,403381,98E+001,38E+1280,99510,99512,274132,403381,98E+001,38E+1280,99510,99512,275132,578481,98E+001,38E+1280,99510,99512,275132,578481,98E+001,38E+1280,99510,99510,99511,5713 <t< td=""><td></td><td>3</td><td>5.88E+00</td><td>3.67E-12</td><td></td><td>3</td><td>0.9963</td><td>0.9966</td><td>19.2900</td><td>20.0090</td></t<>		3	5.88E+00	3.67E-12		3	0.9963	0.9966	19.2900	20.0090
3         4.09E+00         1.84E+12           4         6.36E+00         4.99E+13           5         5.74E+00         1.38E+12           5         5.74E+00         1.38E+12           6         6.36E+00         2.35E+12           5         5.74E+00         1.38E+12           6         6.86E+00         2.2626         2.2582           7         6.86E+00         2.2612         5         0.9954         0.9952         2.13025         17.480           8         6.86E+00         2.2612         5         0.9951         0.9952         0.13025         17.480           7         5.73E+00         2.30E+12         7         4         0.9953         0.9954         2.4592         2.26308           7         5.73E+00         2.2612         7         4         0.9953         0.9954         2.4592         2.26308           7         5.73E+00         3.22E+12         7         3         0.9951         2.7412         2.4083           8         5.58E+00         1.84E+12         9         0.9951         2.7412         2.60935           8         5.85E+00         1.84E+12         9         0.9951         2.61218	Slice 9	4	5.59E+00	1.38E-12	Slice 9	4	0.9966	0.9967	25.1511	24.6520
Sine 1a ASine 1a (A) (A) (A) (A) (A) (A) (A) (A) (A) (A)		5	6.38E+00	1.38E-12		5	0.9973	0.9971	26.8892	26.4528
Silve 1046,36E+004,59E+13Silve 1050,9962,5212,538255,74E+001,38E+1250,99640,99642,40612,406145,73E+002,30E+1260,9960,9960,9962,20702,2030855,73E+002,30E+1260,99510,99500,9962,70702,2030866,89E+002,30E+1260,99510,99500,9962,70702,2030876,89E+002,30E+1260,99500,99500,99502,74102,308486,58E+001,84E+127,56E+003,22E+120,99500,99512,74102,308486,58E+001,84E+1260,99500,99512,74102,74102,741095,58E+001,84E+1270,99510,99512,74102,74102,741096,62E+000,00E+00760,99510,99512,74102,741096,62E+000,00E+00760,99510,99512,62102,751296,72E+002,30E+201,38E+1270,99510,99512,62102,621296,72E+002,30E+201,38E+1270,99510,99512,61202,622996,72E+002,30E+202,30E+202,30E+201,38E+1270,99512,61202,521296,72E+002,30E+202,30E+202,30E+201,38E+12 <td></td> <td>2</td> <td>4.09E+00</td> <td>1.84E-12</td> <td></td> <td>2</td> <td>0.9950</td> <td>0.9952</td> <td>18.4858</td> <td>18.0336</td>		2	4.09E+00	1.84E-12		2	0.9950	0.9952	18.4858	18.0336
46.36E+004.59E+1340.99600.906023.521923.585255.74E+001.38E+1250.99640.906424.00124.00286.68E+002.76E+1286.98540.99540.99542.02502.2530855.89E+002.30E+12869.99540.99540.99542.03052.27052.230885.89E+002.76E+1289.99540.99540.99542.07072.331865.89E+002.76E+1280.99540.99540.99542.77012.731375.86E+001.84E+1280.99540.99540.99542.77012.731385.96E+003.22E+121.84E+129.99540.99542.77112.7671480.518E+001.84E+129.99540.99540.99542.77112.7571393.019E+001.38E+1280.99540.99542.77132.7571395.80E+000.00E+00890.99540.99542.71512.7571395.80E+002.30E+12890.99540.99542.62022.152995.80E+002.30E+12890.99540.99542.62022.152995.80E+002.30E+12890.99540.99542.62022.152995.80E+002.30E+12890.99540.99542.62022.152996.2		3	5.73E+00	9.19E-13	<b>e</b> 1	3	0.9956	0.9959	22.6296	22.0558
1         4.55E+00         1.38E-12         1.	Slice 162	4 6.36E+00 4.59E-13	Slice 162	4	0.9960	0.9960	23.5219	23.5852		
Sine 14         3         6.68E+00         2.76E+12         3         3         0.9951         0.9952         2.01306         2.0290           5         5.89E+00         4.59E+13         5         0.9953         0.9954         2.34549         2.4083           5         5.89E+00         2.76E+12         2         0.9936         0.9940         0.9957         2.3131           6         5.16E+00         1.84E+12         3         0.9952         0.9951         2.2741         2.4079           6         5.58E+00         1.84E+12         3         0.9951         0.9951         2.5742         2.5781           5         5.58E+00         1.84E+12         3         0.9946         0.9947         2.4741         2.17510           5         5.80E+00         0.30E+12         3         0.9946         0.9941         2.17510         2.1513           5         5.80E+00         0.30E+12         3         0.9946         0.9941         2.4614         2.3614           5         0.9951         0.991         2.6242         6.1628         6.1628         6.1628         6.1628         6.1628         6.1628         6.1628         6.1628         6.1628         6.1628         6.162		5	5.74E+00	1.38E-12		5	0.9964	0.9964	24.2061	24.5045
Shice 16445,78E+002,30E+12Shice 16440,99550,99562,27052,230855,89E+004,59E+1355,89E+002,76E+1250,99530,99401,74611,7374847,56E+003,22E+1246,99550,99500,99512,274132,06792,131855,58E+001,84E+1250,99520,99512,274132,06792,17132,067955,58E+001,84E+1220,99570,99570,99571,82711,792166,62E+000,00E+0040,99400,99402,36442,206355,80E+002,30E+1260,99510,99510,99512,66222,612866,62E+000,00E+007,6E+1240,99400,99402,84402,306366,62E+000,00E+007,6E+127,86140,99510,99512,65222,152865,80E+002,30E+127,6E+1240,99510,99512,65292,152866,72E+002,76E+127,6E+127,6E+1230,99510,99512,61622,60292,15287,1121,32E+121,33E+127,36E+102,36E+121,36E+1230,99510,99512,61622,60292,37442,52848,1121,32E+121,32E+121,36E+121,36E+121,36E+121,36E+121,36E+121,36E+121,36E+121,36E+121,36E+12 <td></td> <td>2</td> <td>4.55E+00</td> <td>1.38E-12</td> <td></td> <td>2</td> <td>0.9938</td> <td>0.9942</td> <td>18.0325</td> <td>17.4480</td>		2	4.55E+00	1.38E-12		2	0.9938	0.9942	18.0325	17.4480
4       5,73E+00       2,30E+12       4       0,9955       0,9956       22,705       22,6308         5       5,89E+00       4,59E+13       5       0,9953       0,9954       23,4549       24,083         3       5,16E+00       1,84E+12       3       0,9945       0,9940       0,9940       2,74614       1,73748         4       7,56E+00       3,22E+12       6       0,9950       0,9951       22,7413       24,0679         5       5,58E+00       1,84E+12       6       0,9951       0,9951       0,9951       25,4724       25,7841         3       5,19E+00       1,84E+12       7,9951       0,9937       0,9937       1,8271       1,7921         5       5,80E+00       1,38E+12       7,86       0,9946       0,9944       21,7510       21,5173         5       5,80E+00       0,00E+00       7,6612       7,9951       0,9951       0,9952       18,1550       17,9371         5       5,80E+00       0,30E+12       7,66140       1,38E+12       7,66140       1,38E+12       1,508       0,9951       0,9951       2,66242       2,61298         5       5,20E+00       0,27E+12       2,3156       1,38E+12       1,60951		3	6.68E+00	2.76E-12		3	0.9951	0.9952	20.1306	20.2950
1         4.95E+00         2.76E+12           3         5.16E+00         1.84E+12           4         7.56E+00         3.22E+12           5         5.58E+00         1.84E+12           5         5.58E+00         1.84E+12           4         0.9950         0.9931         2.27413         2.40679           5         5.58E+00         1.84E+12         5         0.9952         0.9937         2.5.724         2.5.7841           5         5.58E+00         1.84E+12         5         0.9952         0.9937         1.8.2731         1.7.9921           6         6.62E+00         0.00E+00         2.30E+12         3         0.9946         0.9949         2.4844         2.3063           5         5.80E+00         2.30E+12         5         0.9951         0.9951         2.66242         2.61298           5         5.80E+00         0.30E+12         5         0.9951         0.9952         1.81550         1.75531           5         5.80E+00         2.30E+12         5         0.9954         0.9954         2.61623         2.60267           5         4.72E+00         2.30E+12         5         0.9964         2.61623         2.60267 <t< td=""><td>Slice 164</td><td>4</td><td>5.73E+00</td><td>2.30E-12</td><td>Slice 164</td><td>4</td><td>0.9955</td><td>0.9956</td><td>22.7705</td><td>22.6308</td></t<>	Slice 164	4	5.73E+00	2.30E-12	Slice 164	4	0.9955	0.9956	22.7705	22.6308
Shee 163.6.6.4.001.8.4E.123.0.9480.9480.7.0570.1.3.1855.5.8E.4.001.8.4E.1250.99520.99530.5.47.40.7.05765.5.8E.4.001.8.4E.1250.99520.99530.9470.7.0710.7.97176.62E.4.000.00E.4001.8.4E.1240.99440.94442.1.7.512.1.7.1386.62E.4.000.00E.4001.8.4E.1250.99510.94442.3.08.1295.80E.4.002.30E.121.8.2F.1250.99510.99512.6.6220.1.28885.72E.4.000.00E.4001.8.2F.1250.99510.99512.6.6220.1.28895.72E.4.000.30E.121.8.2F.1250.99510.99512.6.2922.1.52896.72E.4.000.00E.4001.8.2F.1250.99640.99642.6.2922.1.52896.72E.4.002.30E.121.8.2F.1250.99640.99642.6.2922.1.52896.72E.4.000.00E.4001.8.4F.1250.99640.99642.6.2922.1.91897.62E.4.009.19E.1350.99640.99542.4.1941.1.36797.62E.4.009.19E.131.8.4F.1250.99540.99542.4.1941.1.36797.62E.4.009.19E.131.8.4F.121.8.4F.121.8.4F.121.8.4F.121.8.4F.121.8.4F.121.8.4F.121.8.4F.121.8.4F.12 <td< td=""><td></td><td>5</td><td>5.89E+00</td><td>4.59E-13</td><td></td><td>5</td><td>0.9953</td><td>0.9954</td><td>23.4549</td><td>24.2083</td></td<>		5	5.89E+00	4.59E-13		5	0.9953	0.9954	23.4549	24.2083
Shife 1647.56F+003.22F-12Shife 1640.99500.99512.2.4132.404955.58F+001.84F-1250.99520.99532.547242.578143.91F+001.84F-1250.99370.99371.827311.792146.62F+000.00E+0040.99400.99402.18412.3081255.80F+002.30F-1250.99510.99512.64242.15102.1513655.80F+002.30F-1250.99510.99512.64242.15102.1513755.80F+002.30F-1250.99510.99512.64242.15102.151386.22F+000.00E+002.27E+130.99510.99510.99512.64242.1519965.70F+002.30F-1250.99510.99512.64242.15192.1513967.70F+002.30F-1250.99510.99512.64242.15192.1513967.79F+002.30F-1250.99610.99612.64242.15162.1513967.99F+000.91F+1360.99610.99612.04172.15132.1713977.45F+009.19F+1350.99410.99510.99512.14192.1414977.45F+009.19F+1350.99410.99510.99512.14592.1418977.45F+00		2	4.95E+00	2.76E-12		2	0.9936	0.9940	17.4614	17.3748
4       7,56E+00       3,22E-12       4       0,9950       0,9951       22,7413       24,0679         5       5,58E+00       1,84E-12       5       0,9952       0,9953       25,4724       25,7811         8       5,19E+00       1,84E-12       5       0,9952       0,9937       18,2731       17,9921         8       6,62E+00       0,00E+00       6       6,62E+00       0,00E+00       4       0,9940       0,9944       21,7510       21,5713         6       6,62E+00       0,00E+00       2,30E+12       6,9951       0,9951       26,622       26,1298         7       5,80E+00       2,30E+12       6,9954       0,9951       26,624       26,1298         8       5,22E+00       0,00E+00       2,76E+12       5       0,9954       0,9951       26,625       21,528         9       4,72E+00       2,30E+12       5       0,9954       0,9954       24,9767       24,8232         5       6,379E+00       1,88E+12       5       0,9964       0,9954       24,1950       24,1950       24,1950       24,1951       24,1952       24,0267       24,8232         5       7,30E+00       0,91F+13       5       0,9947       0		3	5.16E+00	1.84E-12		3	0.9945	0.9948	20.7057	21.3318
2         3.91E+00         1.84E-12         2         0.9937         0.9937         18.2731         17.9921           3         5.19E+00         1.38E-12         3         0.9946         0.9944         21.7510         21.5713           4         6.62E+00         0.00E+00         4         0.9946         0.9940         23.4844         23.2063           5         5.80E+00         2.30E-12         6         0.9951         0.9951         2.66242         2.61298           5         5.22E+00         0.00E+00         2.427E+00         2.07E-12         3         0.9958         0.9961         2.26259         21.5298           4         5.70E+00         2.30E-12         5         0.9960         0.9964         24.9767         2.48232           5         4.72E+00         2.30E-12         5         0.9960         0.9964         26.1623         2.60267           5         4.72E+00         2.30E-12         5         0.9960         0.9964         26.1623         2.60267           5         7.80E+00         9.19E-13         5         0.9947         0.9945         2.4194         2.1.1367           5         7.80E+00         9.19E-13         5         0.9948	Slice 165	4	7.56E+00	3.22E-12	Slice 165	4	0.9950	0.9951	22.7413	24.0679
Slice 160         3         5.19E+00         1.38E+12         3         0.9946         0.9944         2.1.751         2.1.751           5         5.80E+00         0.00E+00         4         0.9949         0.9949         2.3.4844         2.3.0613           6         5.80E+00         2.3.0E+12         5         0.9951         0.9951         2.6.6242         2.6.1298           7         5.22E+00         0.00E+00         2.5         0.9958         0.9961         2.6.6242         2.6.298           6         5.22E+00         0.38E+12         3         0.9958         0.9964         2.6.629         2.1.528           6         5.70E+00         2.30E+12         5         0.9960         0.9964         2.6.623         2.6.027           7         4.72E+00         2.30E+12         5         0.9960         0.9964         2.6.1623         2.6.027           8         6.20E+00         0.30E+12         5         0.9960         0.9964         2.6.1623         2.6.027           9         7.26E+00         3.22E+12         5         0.9947         0.9945         2.4.194         2.1.367           8         5.86E+00         1.38E+12         5         5         0.9948		5	5.58E+00	1.84E-12		5	0.9952	0.9953	25.4724	25.7841
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		2	3.91E+00	1.84E-12		2	0.9937	0.9937	18.2731	17.9921
4       6.62E+00       0.00E+00       4       0.9949       0.9949       23.4844       23.2063         5       5.80E+00       2.30E-12       5       0.9951       0.9951       26.6242       26.1298         8       5.22E+00       0.00E+00       38E-12       3       0.9958       0.9961       22.6259       21.5298         4       5.70E+00       2.30E-12       3       0.9958       0.9961       22.6259       21.5298         5       4.72E+00       2.30E-12       5       0.9960       0.9964       24.9767       24.8323         6       4.72E+00       2.30E-12       5       0.9960       0.9964       26.1623       26.0257         8       6.20E+00       0.30E+12       5       0.9960       0.9964       24.192       21.1367         5       7.80E+00       0.30E+10       5.16E+163       6.9963       0.9935       17.8610       17.754         6       7.45E+00       9.19E-13       5       0.9947       0.9952       24.1990       24.4890         5       7.80E+00       1.38E-12       5       5.79E+00       0.30E+12       1.3616       1.4649       1.9995       2.9993       1.8.6405       1.7.648		3	5.19E+00	1.38E-12		3	0.9946	0.9944	21.7510	21.5713
2         2.27E+00         0.00E+00           3         5.22E+00         1.38E+12           4         5.70E+00         2.76E+12           5         4.72E+00         2.30E+12           5         4.72E+00         2.30E+12           4         0.9964         2.49767           5         4.72E+00         2.30E+12           5         4.72E+00         2.30E+12           3         6.20E+00         0.00E+00           4         7.45E+00         9.19E+13           5         7.80E+00         9.19E+13           5         7.80E+00         9.19E+13           5         7.80E+00         9.19E+13           6         7.80E+00         9.19E+13           6         7.80E+00         9.19E+13           5         5.78E+00         3.22E+12           5         5.79E+00         1.38E+12           6         0.9948         0.9948         0.9948           7.60E+00         1.38E+12           8         6.0947         0.9952         2.14940           8         6.09947         0.9948         0.9948         2.2296           9.19E+13         6         0.9953	Slice 166	6	Slice 166	4	0.9949	0.9949	23.4844	23.2063		
Slice 167       3       5.22E+00       1.38E-12       3       0.9958       0.9961       2.26259       2.15298         4       5.70E+00       2.76E-12       4       0.9963       0.9964       2.49767       2.48232         5       4.72E+00       2.30E-12       5       0.9960       0.9964       2.61623       2.60267         5       4.72E+00       1.84E-12       5       0.9960       0.9964       2.61623       2.60267         6       6.20E+00       0.00E+00       8       8       8       0.9947       0.9945       2.24194       21.1367         6       7.80E+00       9.19E-13       5       0.9947       0.9945       2.44909       2.44890         5       7.80E+00       9.19E-13       5       0.9947       0.9948       0.9948       2.2996       21.4387         5       5.79E+00       0.00E+00       5       0.9948       0.9948       2.2201       2.37089         6       5.79E+00       0.00E+00       5       0.9953       0.9948       2.2201       2.37089         5       5.79E+00       0.00E+00       5       0.9953       0.9948       2.2203       2.49890         8       6.00E+00 <td></td> <td>5</td> <td>5.80E+00</td> <td>2.30E-12</td> <td></td> <td>5</td> <td>0.9951</td> <td>0.9951</td> <td>26.6242</td> <td>26.1298</td>		5	5.80E+00	2.30E-12		5	0.9951	0.9951	26.6242	26.1298
Slice 167     4     5.70E+00     2.76E-12     4     0.9963     0.9964     24.9767     24.8232       5     4.72E+00     2.30E-12     5     0.9960     0.9964     26.1623     26.0267       5     3.79E+00     1.84E-12     5     0.9960     0.9945     2.24194     21.1367       6     7.45E+00     0.00E+00     4     0.9947     0.9945     2.24194     21.1367       6     7.80E+00     9.19E-13     6     0.9947     0.9952     24.5909     24.4800       7     7.80E+00     9.19E-13     5     0.9947     0.9952     24.5909     24.4800       8     7.80E+00     9.19E-13     5     0.9947     0.9952     24.5909     24.4800       8     5.88E+00     1.38E-12     5     0.9947     0.9948     0.9948     22.2966     21.4387       9     5.88E+00     1.38E-12     5     0.9953     0.9948     0.9948     22.0291     23.0781       9     5.79E+00     0.00E+00     5     0.9953     0.9948     25.2023     24.9809       9     5.79E+00     0.00E+00     5     0.9953     0.9948     25.2023     24.9809       9     5.79E+00     0.00E+00     5     0.9953		2	2.27E+00	0.00E+00		2	0.9954	0.9952	18.1550	17.9531
4       5.70E+00       2.76E-12       4       0.9963       0.9964       24.9767       24.8232         5       4.72E+00       2.30E-12       5       0.9960       0.9964       26.1623       26.0267         8       6.20E+00       0.00E+00       8       8       0.9947       0.9945       22.4194       21.1367         9       7.45E+00       9.19E-13       6       0.9947       0.9952       24.5909       24.4980         16       7.80E+00       9.19E-13       5       0.9947       0.9952       24.5909       24.4980         16       7.80E+00       9.19E-13       5       0.9947       0.9952       24.5909       24.4980         16       7.80E+00       9.19E-13       5       0.9947       0.9952       24.5909       24.4980         17.64E+00       3.22E-12       1.38E-12       1.38E-12       1.38E-12       1.48E-12       0.9948       0.9948       22.296       21.4387         18       8.36E+00       1.38E-12       5       0.9953       0.9954       25.203       24.9809         19       5.79E+00       0.00E+00       5       0.9953       0.9954       25.203       24.9809         19       1.38E		3	5.22E+00	1.38E-12	CI: 1.67	3	0.9958	0.9961	22.6259	21.5298
2         3.79E+00         1.84E+12         2         0.9935         0.9935         17.8610         17.7754           3         6.20E+00         0.00E+00         4         0.9947         0.9945         22.4194         21.1367           4         7.45E+00         9.19E-13         4         0.9948         0.9950         23.1925         23.0741           5         7.80E+00         9.19E-13         5         0.9947         0.9952         24.5909         24.4890           8         5.80E+00         3.22E-12         5         0.9947         0.9952         22.0291         23.0741           3         5.88E+00         1.38E-12         3         0.9948         0.9948         22.2996         21.4387           5         5.79E+00         0.00E+00         5         0.9953         0.9954         25.203         24.9809           5         5.79E+00         0.00E+00         5         0.9953         0.9954         25.203         24.9809           5         5.79E+00         0.00E+00         5         0.9953         0.9946         20.9713         20.9983           6         0.9945         0.9946         20.9713         20.9984         22.2872         22.4437 <td>Slice 167</td> <td>4</td> <td>5.70E+00</td> <td>2.76E-12</td> <td>Slice 167</td> <td>4</td> <td>0.9963</td> <td>0.9964</td> <td>24.9767</td> <td>24.8232</td>	Slice 167	4	5.70E+00	2.76E-12	Slice 167	4	0.9963	0.9964	24.9767	24.8232
3         6.20E+00         0.00E+00         Alere 168         3         0.9947         0.9945         22.4194         21.1367           4         7.45E+00         9.19E-13         4         0.9948         0.9950         23.1925         23.0741           5         7.80E+00         9.19E-13         5         0.9947         0.9952         24.5909         24.4890           6         7.26E+00         3.22E-12         2         0.9939         0.9938         18.6405         17.6448           5         5.88E+00         1.38E-12         3         0.9951         0.9952         22.0291         23.7089           6         5.79E+00         0.00E+00         5         0.9953         0.9954         25.203         24.9899           8         6.40E+00         1.84E-12         1         2         0.9953         0.9954         25.203         24.9899           5         5.79E+00         0.00E+00         5         0.9953         0.9954         25.2203         24.9899           8         4.60E+00         9.19E-13         2         0.9947         0.9946         20.9713         20.9943           8         4.60E+00         9.19E-13         3         0.9942         0.		5	4.72E+00	2.30E-12		5	0.9960	0.9964	26.1623	26.0267
Slice 168       A       7.45E+00       9.19E-13       A       0.9948       0.9950       23.1925       23.0741         5       7.80E+00       9.19E-13       5       0.9947       0.9952       24.5909       24.4890         A       7.26E+00       3.22E-12       5       0.9948       0.9948       0.9948       22.296       21.4387         B       5.88E+00       1.38E-12       3       0.9948       0.9952       22.0291       23.7089         5       5.79E+00       0.00E+00       5       0.9953       0.9954       25.2203       24.9809         2       2.19E+00       2.30E-12       2       0.9947       0.9948       20.991       23.0291       23.7089         3       4.60E+00       9.19E-13       2       0.9953       0.9954       25.2203       24.9809         Slice 38       4       6.9947       0.9946       20.9713       20.9083         4       0.9945       0.9940       22.2872       22.4437         5       3.91E+00       2.30E-12       3       3       0.9945       0.9947       2.9447       2.9447		2	3.79E+00	1.84E-12		2	0.9935	0.9935	17.8610	17.7754
4       7.45E+00       9.19E-13       4       0.9948       0.9950       23.1925       23.0741         5       7.80E+00       9.19E-13       5       0.9947       0.9952       24.5909       24.4890         8       5.80E+00       3.22E-12       2       0.9939       0.9938       18.6405       17.6448         3       5.88E+00       1.38E-12       3       0.9948       0.9948       22.2996       21.4387         4       0.9951       0.9952       22.0291       23.7089       23.7089       23.7089         5       5.79E+00       0.00E+00       5       0.9953       0.9954       25.2203       24.9809         2       2.19E+00       2.30E-12       2       0.9947       0.9946       20.9713       20.9083         3       4.60E+00       9.19E-13       2       0.9947       0.9940       22.2872       22.4437         5lice 38       3       4.0945       0.9947       0.9947       23.3119       23.1477	Clice 160	3	6.20E+00	0.00E+00	Clice 160	3	0.9947	0.9945	22.4194	21.1367
2         7.26E+00         3.22E-12           3         5.88E+00         1.38E-12           4         8.36E+00         1.84E-12           5         5.79E+00         0.00E+00           2         2.19E+00         2.30E-12           3         4.60E+00         9.19E-13           4         3.91E+00         2.30E-12	Slice 168	4	7.45E+00	9.19E-13	Slice 168	4	0.9948	0.9950	23.1925	23.0741
3       5.88E+00       1.38E-12       3       0.9948       0.9948       22.296       21.4387         4       8.36E+00       1.84E-12       4       0.9951       0.9952       22.0291       23.7089         5       5.79E+00       0.00E+00       5       0.9953       0.9946       20.9713       20.9083         8       4.60E+00       9.19E-13       3       0.9942       0.9940       22.2872       22.4437         8       3.91E+00       2.30E-12       3       0.9945       0.9947       0.9940       22.2872       22.4437		5	7.80E+00	9.19E-13		5	0.9947	0.9952	24.5909	24.4890
Slice 169       4       8.36E+00       1.84E-12       4       0.9951       0.9952       22.0291       23.7089         5       5.79E+00       0.00E+00       5       0.9953       0.9954       25.2203       24.9809         8       2       2.19E+00       2.30E-12       2       0.9947       0.9946       20.9713       20.9083         8       4.60E+00       9.19E-13       8       0.9945       0.9940       22.2872       22.4437         4       3.91E+00       2.30E-12       8       1       0.9945       0.9947       23.3119       23.1477		2	7.26E+00	3.22E-12		2	0.9939	0.9938	18.6405	17.6448
4       8.36E+00       1.84E-12       4       0.9951       0.9952       22.0291       23.7089         5       5.79E+00       0.00E+00       5       0.9953       0.9954       25.2203       24.9809         2       2.19E+00       2.30E-12       2       0.9947       0.9946       20.9713       20.9083         Slice 38       3       4.60E+00       9.19E-13       3       0.9945       0.9947       22.2872       22.4437         4       0.391E+00       2.30E-12       3       0.9945       0.9947       23.3119       23.1477		3	5.88E+00	1.38E-12	Cline 160	3	0.9948	0.9948	22.2996	21.4387
2         2.19E+00         2.30E-12         2         0.9947         0.9946         20.9713         20.9083           3         4.60E+00         9.19E-13         3         0.9942         0.9940         22.2872         22.4437           4         3.91E+00         2.30E-12         3         0.9945         0.9947         23.3119         23.1477	Slice 169	4	8.36E+00	1.84E-12	Slice 169	4	0.9951	0.9952	22.0291	23.7089
3         4.60E+00         9.19E-13         3         0.9942         0.9940         22.2872         22.4437           4         3.91E+00         2.30E-12         4         0.9945         0.9947         23.3119         23.1477		5	5.79E+00	0.00E+00		5	0.9953	0.9954	25.2203	24.9809
Slice 38 4 3.91E+00 2.30E-12 4 0.9945 0.9947 23.3119 23.1477		2	2.19E+00	2.30E-12		2	0.9947	0.9946	20.9713	20.9083
4 3.91E+00 2.30E-12 4 0.9945 0.9947 23.3119 23.1477		3	4.60E+00	9.19E-13	CI:. 20	3	0.9942	0.9940	22.2872	22.4437
5 3.89E+00 2.30E-12 5 0.9950 0.9952 23.4757 23.6046	Slice 38	4	3.91E+00	2.30E-12	Slice 38	4	0.9945	0.9947	23.3119	23.1477
		5	3.89E+00	2.30E-12		5	0.9950	0.9952	23.4757	23.6046

# 6. CONCLUSION

In this paper, the PLBA algorithm based multilevel thresholding using Otsu's criterion is discussed. T2 weighted brain MR axial plane images are applied as test images. It is observed that the PLBA is higher in terms of the fitness value (Otsu) and low standard deviation for all test images. The uniformity measure of PLBA based multilevel thresholding is mostly higher than HS and it represents the quality of the segmentation algorithm. The segmented image yields more information of the image when the number of threshold levels increases. The statistical performance of the PLBA and HS is evaluated by using one-way ANO-VA. The test showed that there is a significant difference in standard deviation for both algorithms even though there exists no significant difference of the objective value and uniformity between the PLBA and HS. This proves that the PLBA is more stable than HS. A higher threshold level implies the effectiveness of brain MRI images to differentiate between normal and abnormal tissues.

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